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# Model Testing and Performance Comparison of Plastic and Metal Tidal Turbine Rotors

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## Abstract

Experimental model tests were conducted to predict the performance of two sets of metal and plastic bi-directional tidal turbine rotors. This test program aims to provide reliable and accurate measurement data as references for developers, designers and researchers on both model and full scale. The data set presented in this paper makes available the detailed geometry and motion parameters that are valuable for numerical tools validation. A rotor testing apparatus that was built using an off-the-shelf K&R propeller dynamometer, its configuration, testing set-up, calibration of the apparatus and data acquisition are described. Comparison analysis between the metal and plastic rotors hydrodynamic performance in terms of torque, drag and derived power and drag coefficients are also presented. The results show a substantial decrease in maximum power performance for the plastic ro-

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tors — about 40% decrease at a tip speed ratio of around 3.0, compared with rigid metal rotors. The plastic rotors have also a much higher cut-in speed. It showed that materials for rotor models with low rigidity such as polyamide (nylon) produced by selective laser sintering (SLS) systems may substantially under-predict power generation capacity. As a result, they are considered unsuitable for rotor model performance evaluation.

*Keywords:* metal and plastic rotor testing, bi-directional turbine, HATT, HACT

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## 1 Nomenclature

Symbol	Description	Units
$D$	Rotor diameter,	$m$
$R$	Rotor radius,	$m$
$A$	Area of rotor disk, $A = \pi R^2$	$m^2$
$\alpha_p$	Geometric angle of blade section	Rad or deg
$\alpha'_v$	Resultant angle of inflow velocity with added induced velocity,	Rad or deg
$\alpha_o$	Angle of zero lift of blade section,	Rad or deg
$\alpha_e$	Effective angle of attack of blade section,	Rad or deg
$c_{0.7R}$	Blade chord length at $r = 0.7R$	$m$
$n$	Rotor shaft speed,revolution per second,	rpm
$N$	Rotor shaft speed,revolution per minute,	RPM
$R$	Rotor radius,	$m$
$Z$	Number of blades	
$V_{in}$	Tidal inflow speed at rotor disk plane,	$m/s$

$\rho$	Fluid density,	$kg/m^3$
$\mu$	Fluid dynamic viscosity,	$N \cdot s/m^2$
$\nu$	Fluid kinetic viscosity, $\mu/\rho$ ,	$m^2/s$
$p$	Blade pitch,	$m$
$p_D$	Blade pitch diameter ratio	
$p_{D_{0.7R}}$	Blade pitch diameter ratio at $r = 0.7R$ ,	
$V_{resultant}$	$= \sqrt{(0.7R\omega)^2 + V_{in}^2}$ , Resultant velocity at $r = 0.7R$ ,	$m/s$
$V_a$	Inflow velocity,	$m/s$
$V'_a$	Inflow velocity with added induced velocity,	$m/s$
$V_t$	Induced tangential velocity at the rotor disk plane,	$m/s$
$V_x$	Induced axial velocity at blade section	$m/s$
$EAR$	Rotor disk solidity $EAR = \frac{A_{rotor}}{\pi R^2}$	
$TSR$	Tip speed ratio $TSR = \frac{2\pi nR}{V_{in}}$	
$Rn$	Reynolds number, $Rn = \frac{VL}{\nu} = \frac{\sqrt{(0.7R\omega)^2 + V_{in}^2} c_{0.7R}}{\nu}$	
$Q$	Shaft torque,	$N \cdot m$
$T$	Thrust or drag on shaft	$N$
$Q_{adj}$	Adjusted torque measurement,	$N \cdot m$
$Q_{measured}$	Measured torque,	$N \cdot m$
$Q_{tare}$	Tare torque,	$N \cdot m$
$Q_0$	Torque reading at zero torque,	$N \cdot m$
$C_t$	Rotor thrust/drag coefficient, $C_t = \frac{T}{\frac{1}{2}\rho V_a^2 A}$	
$C_{pow}$	Rotor power coefficient, $C_{pow} = \frac{P}{\frac{1}{2}\rho V_a^3 A}$	

## 2 1. Introduction

3 With the rapid development of renewable energy turbine science and tech-  
4 nologies, more and more horizontal axis turbine rotors were tested in both  
5 model and full scale, to assess their power coefficient. Publications providing  
6 a complete suite of geometry and motion data that could be conveniently and  
7 effectively used as a methodical series, are rarely found. The best examples  
8 existing include a set of measurement data from a full scale trial of a wind  
9 turbine rotor [5], a set of experimental testing data for an unidirectional-  
10 bladed tidal turbine rotor model with controllable pitch [4], and a full suite  
11 of measured data, detailed geometric and motion parameters along with a  
12 detailed description of the testing apparatus in a recent work [13]. These  
13 have effectively provided for the demand for the availability of physical mea-  
14 surement data for numerical code validation, research and development and  
15 industrial design reference.

16 Tidal currents in terms of ebb and flood tides, are bi-directional. Hori-  
17 zontal axis tidal turbines need to be designed to operate in both directions.  
18 As summarized in a recent work [12], there are three basic configurations for  
19 tidal turbines to work in bi-directional currents: 1) An unidirectional turbine  
20 which "weather vanes" (at about  $180^\circ$ ) so that it always faces the current.  
21 This kind of turbines uses unidirectional blade; 2) A bi-directional turbine  
22 with unidirectional blade section achieved by reversing blade pitch angle  
23 ( $180^\circ$ ); and 3) A bi-directional rotor with fully symmetrical blade section  
24 that operates identically in both tidal flow directions with shaft rotating in  
25 opposing directions. Each of these individual configurations has advantages  
26 and disadvantages; for example, the bi-directional blade of the 3rd configu-

27 ration will result in a reduced hydrodynamic performance but it saves the  
28 mechanical and electronic control needed for either alternating the orienta-  
29 tion of the turbine alternating the pitch of the blades at about  $180^\circ$ . For  
30 the 3rd tidal turbine configuration, a comprehensive numerical simulation  
31 and optimization for horizontal axis turbines operating under the tidal flow  
32 conditions of Minus passage, the Bay of Fundy was completed with emphases  
33 on hydrodynamic performance [12] and optimization for structural strength  
34 and integrity [15], under a research project funded by Natural Resources  
35 Canada (NRCan). As a result of over 15,000 data runs and analysis in the  
36 simulation and optimization processes completed [12] using a time-domain  
37 and multiple-body panel method, 10 rotors were initially recommended for  
38 further experimental model testing. For the rotor series testing program [14],  
39 10 plastic rotors and 7 metal rotor models were made. Hydrodynamic char-  
40 acteristics of the 7 metal rotors were presented in a recent work [13].

41 The use of plastic materials for rotor model testing has great advantages  
42 in terms of meeting client requirements to minimize cost and manufacture  
43 time. For example, depending on roughness and manufacture accuracy re-  
44 quirement, the cost of the plastic rotor model is approximately  $1/10th$  of the  
45 aluminium rotor with the same size (\$200 versus \$2,000) and about  $1/25th$   
46 of the stainless steel rotor models (\$200 versus \$5,000). The time required to  
47 manufacture a plastic rotor via a 3D printer is about  $1/10th$  of the aluminium  
48 one via a CNC machine (1 hours versus 10 hours). In the past few decades,  
49 computer-aided manufacturing of rotor models using CNC and 3D printing  
50 technology has advanced dramatically, along with the lighter and much lower  
51 cost materials (less than 10% total cost compared with CNC metal rotors).

52 While rotor models produced by 3D printing for demonstration and showcase  
53 become more and more popular, there have been wide instances and exam-  
54 ples of using 3D printers to produce rotors for hydrodynamic performance  
55 model testing, especially for self-propulsion tests, for example, at co-authors  
56 institutions, National Research Council Canada and University of Tasmania,  
57 Australia and their domestic maritime research communities.

58 Depending on particular 3D printers, materials used for rotor model pro-  
59 duction have a wide variety of strength properties. Hydrodynamic perfor-  
60 mance of rotors made of the sintered material similar to Nylon 12, compared  
61 with the much more rigid metal rotors could be an important reference in  
62 decision making for rotor model manufacture for performance testing. This  
63 paper presents the measured drag and power coefficients and comparison be-  
64 tween these two sets of aircraft grade aluminium and sintered material similar  
65 to Nylon 12 [1]. A complete set of geometry and testing condition details  
66 and the design of fabrication of the test apparatus were also presented.

67 This paper aims to produce the following outcomes:

- 68 • To provide a complete set of measurement and geometry data for the  
69 two sets of bi-directional turbine rotor models for numerical code vali-  
70 dation.
- 71 • To identify the cause of the hydrodynamic performance degradation  
72 of the plastic rotors by analysing the local flow condition of the blade  
73 sections.
- 74 • To shed some light on stall caused performance reduction due to flex-  
75 ibility of nylon materials and the selection of materials of rotors for

76 propulsion and energy generation in model design, manufacture, and  
77 testing.

### 78 *1.1. The Rotor Models*

79 As part of a larger research program, the authors developed a systematic  
80 series of ten different rotor models [12]. The test program was conducted in  
81 two phases. Phase 1 identified the effect of pitch, pitch distribution, solidity  
82 and Reynolds numbers on the power generation performance of seven rotors  
83 in this series, all fabricated of metal (aircraft grade aluminium), as reported  
84 in [13]. As previously mentioned, an aim of the present study (Phase 2) is to  
85 identify and compare the performance of metal and plastic rotors, whereby  
86 further experiments were performed on two of the seven rotors previously  
87 published [13].

88 There was a consideration to avail of the possibility of testing at the Cav-  
89 itation Tunnel at the National Research Council Canada (NRC) St. John's.  
90 The test section of the NRC cavitation tunnel is  $0.5m \times 0.5m$ . The diameter  
91 of the rotors were limited to around 200 mm by the current technology of the  
92 selective laser sintering (SLS) systems, so called 3D printers at the time when  
93 they were made (around 2010). Based on these limitations, the diameter of  
94 the rotors was taken as 0.23 m. The two plastic rotors were produced by  
95 an SLS system, i.e., a 3D printer, made of polyamide (similar to Nylon 12)  
96 material. The rated ultimate tensile strength of the polyamide is 43 MPa but  
97 the rigidity is rather low with that much tensile strength. To increase the  
98 rigidity, rotor blade sectional thickness was increased by 50% compared with  
99 the full scale (20m diameter) for both plastic and metal rotors to maintain  
100 the same design hydrodynamic characteristics of the blade sections. The two

101 metal rotors were made using computer numerical control (CNC) of aircraft  
 102 grade aluminium (6061 series) by Danford Engineering, Victoria, Australia.  
 103 The two plastic rotors were made at Memorial University of Newfoundland  
 104 along with other 8 plastic rotors. These two plastic rotors presented in this  
 105 work have the identical geometry of the corresponding metal rotors.

106 Table 2 lists the key geometry parameters of the rotor model sets. The  
 107 pitch ratio is measured at  $0.7R$  and  $D_h/D$  is the ratio of the hub diameter  
 108 to rotor diameter.

Table 2: Key geometry parameters of the rotors

Rotor No.	$D_m(m)$	$p_D$	EAR	$D_h/D$
2	0.23	0.31	0.80	0.15
3	0.23	0.27	0.80	0.15

109 The detailed planform geometry and blade sectional offsets of these 2  
 110 sets of rotor models, as part of the input file for the panel method code,  
 111 Propella [11], used for numerical simulation and optimization are provided  
 112 in full in [13].

113 The solidity  $EAR$  of these rotors are very large ( $EAR = 0.8$ ). Earlier  
 114 design and optimization work completed numerically and presented in [12]  
 115 developed a series of ten rotors in which EAR ranges from 0.4 to 0.8. To  
 116 perform a fair and accurate comparison between the plastic and metal rotors,  
 117 the geometry and the testing conditions of the corresponding rotors must be  
 118 the same. In model testing to obtain a relatively large Reynolds number in  
 119 order to minimize or eliminate Reynolds effect, the 0.23 m rotors must rotate

120 fast with a fast inflow speed so this in combination will produce a large  
 121 Reynolds number and desired  $TSR$ . However, plastic rotors with a small  
 122  $EAR$  have poor strength and an inability to cope with the high rotation  
 123 speed and fast inflow speed. Therefore, only the plastic rotors with the  
 124 largest  $EAR$  of 0.8 were tested.

125 Figure 1 show the surface mesh and the metal rotor models. As it can  
 126 be seen in Table 2, rotors no. 2 and 3 have the same solidity, diameter, and  
 hub diameter, but vary slightly in pitch ratio.

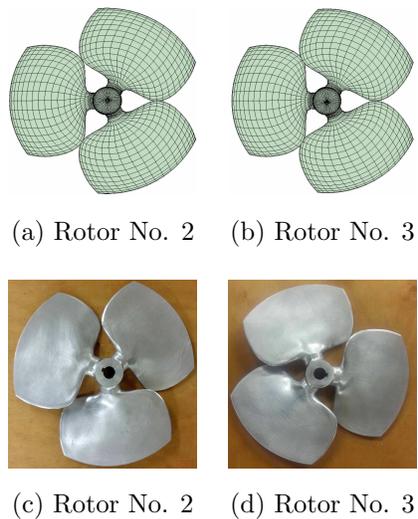


Figure 1: Metal rotors No. 2 and 3

127  
 128 The root sections were designed to be perfectly circular, because other  
 129 sectional shape at the very small radius locations were deemed to contribute  
 130 more drag than power. Circular root sections will have a uniform strength  
 131 in any bending direction (spindle torque, in-plane and out-of-plane bending  
 132 moment — for detail, see [15]). The circular root section and a small hub

133 diameter in combination will save materials as well, if the full scale rotor hub  
134 is designed and made from a billet of material.

135 Numerically, the surface mesh generated by code Propella at the blade  
136 root requires pitch alignment so the root sections had a very large pitch to  
137 obtain a perfect connection between the adjacent panels on the hub and blade  
138 root. The code requires nearly the same local panel corner point coordinates  
139 ( $1.0E10^{-8}$  in error) as the coordinates of the neighbour panels to determine  
140 the adjacent panels and thus to obtain the doublet velocity potential by  
141 taking finite difference derivatives across the neighbour panels on both hub  
142 and blade root. As the first 7 blade sections are all circular, their pitch value  
143 does not affect the performance of the rotor. Streamline sections start at  
144 the 8th section, at  $r/R = 0.2$ . This means that if the hub diameter ratio  
145 increases from 0.15 to 0.2, except for little difference in drag (added drag  
146 due to a larger hub diameter), power performance of the rotor will basically  
147 remain unchanged.

148 Figure 2 shows the plastic rotors No. 2 and 3.

149 In the code Propella, a two-way spline scheme for the blade surface con-  
150 tour was established [9] and used to interpolate and generate the blade sur-  
151 face, in terms of a prescribed number of chordwise and spanwise intervals in  
152 the input file for the code to generate rotor surface panels.

## 153 **2. Test Apparatus, Calibration and Setup**

### 154 *2.1. Test Apparatus*

155 A new rotor testing apparatus was specially designed and built. Only  
156 a very brief introduction to the structure, configuration and setup of the

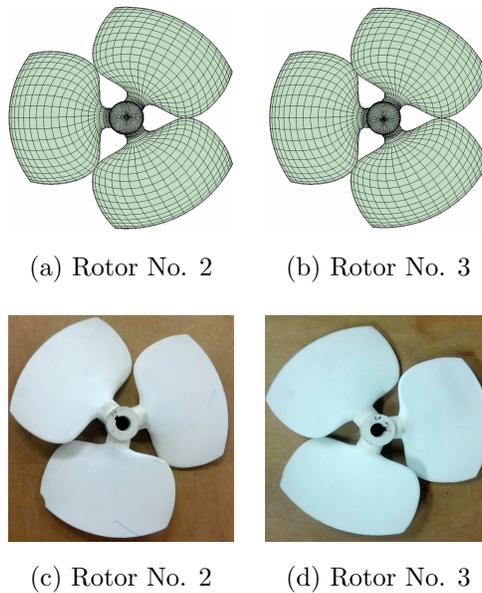


Figure 2: Plastic rotors No. 2 and 3

157 apparatus is given here.

158 Figure 3 shows the internal assembly and individual components of the  
 159 opensboat for this work.

160 In figure 3, from bottom to top, is the nylon seat (in figure 3b) to provide  
 161 a floating mount with torque and thrust retainer, the motor (in figure 3c),  
 162 the universal shaft coupling, the K&R propeller dynamometer (in figure 3d),  
 163 the end shaft coupling and drag retainer, and the cone cap (in figure 3e) of  
 164 the opensboat casing.

165 The capacities of the R31 K&R dynamometer are 4 Nm torque and 100  
 166 N thrust/drag. It was the smallest K&R dynamometer among the 4 K&R  
 167 dynamometers available at Australian Maritime College (AMC). As will be  
 168 discussed in section 3, a smaller torque capacity of about 2 Nm and the

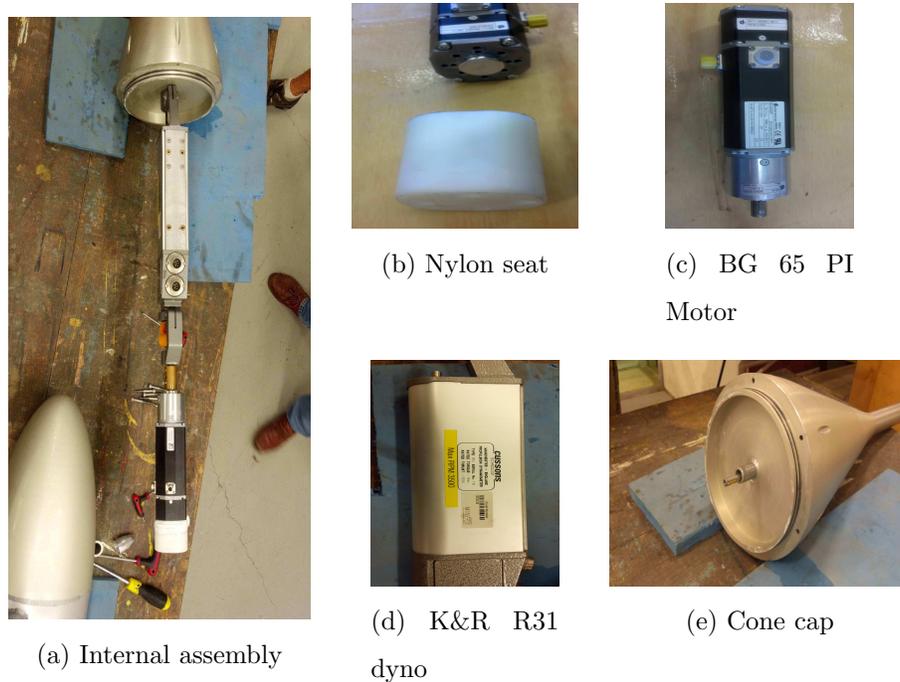


Figure 3: Internal assembly of the opensboat

169 same thrust capacity would be ideal for the rotor model working condition,  
 170 controller ampere rating, motor shaft speed limit and the available carriage  
 171 speed of the tow tank.

172 The motor used is a Dunkermotoren BG 65 PI. It has 2 sets of cable  
 173 connections, the 12-pin and 5-pin ones [6]. The 12-pin connection is power  
 174 signal cable for power and speed input and the 5-pin connection is service  
 175 signal for PC. The motor gear box ratio is 3:1. Motor controller amperage  
 176 rate is 8A. The motor shaft speed limit is 6000 RPM, so the maximum  
 177 allowable rotor shaft speed is 2000 RPM, about 33 rps.

178 The control of the motor is realized by proprietary software that permits

179 up to 8 speeds ( $2^3$ ) prescribed on computer. These parameters of the 8  
180 speeds are loaded in to the motor's circuitry from the software. The speeds  
181 are obtained by sending a corresponding binary code to a stored speed, which  
182 are manually set in the GUI of the software on PC. A binary box was created  
183 by AMC and was used to send the binary code real time on the fly. The  
184 shaft speed, when no binary signal input, is also controlled at zero. The  
185 rotor shaft speed does not have an indexing feedback which would make  
186 more automation and efficiency in data acquisition and processing.

187 Figure 4 shows the opensboat assembly and its setup mounting on the  
carriage over the AMC towing tank.



(a) Opensboat assembly (b) Opensboat setup

Figure 4: Opensboat assembly and test setup

188

189 The casing of the opensboat is made of aircraft grade aluminium. The  
190 mid part of the casing is made of aluminium plate that was wrapped and

191 welded together. The cone cap is a solid one-piece.

192 The two vertical tubes that supported the opensboat (seen in Figure 4a)  
193 were not covered with streamlined shells as planned. A substantial vortex  
194 induced vibration and transverse oscillation occurred at carriage speeds in  
195 excess of 2 m/s. The carriage speed was initially set to 1 m/s and no ob-  
196 vious vibration was noticed. However, to improve the accuracy of the mea-  
197 surements by increasing measured torque and hence torque sensitivity and  
198 reducing the Reynolds number effect, it was set at 1.5 m/s for most data  
199 points. A tension cable was applied to wrap around the mid part of the  
200 opensboat and be anchored across the mounting seat of the towing tank car-  
201 riage. These significantly reduced traverse motion, vortex induced vibration  
202 and self-excitation.

203 The AMC towing tank is 100 m long, 3.5 m wide, 1.5 m deep. The  
204 maximum carriage speed of the towing tank is 4.6 m/s [2].

205 The rotor is placed upstream with a shaft immersion depth of 0.75 m (half  
206 tank depth) to reduce the free surface and bottom wall effect to minimum.  
207 The gondola (opensboat body) is about 5-diameter downstream of the rotor  
208 plane — the distance is far enough to reduce the effect on torque and hence  
209 power coefficient measurement on the rotor to the minimum, that could be  
210 possibly created by the interaction between the shed vortices and the gondola  
211 body.

## 212 *2.2. Dynamometer Calibration and Data Acquisition Setup*

213 The most important hydrodynamic performance characteristics of a tur-  
214 bine rotor is its power coefficient versus tip speed ratio  $TSR$ . Another hydro-  
215 dynamic property to measure is the drag/thrust coefficient. These coefficients

216 and the  $TSR$  are, for turbine rotors, usually expressed as:

$$C_{pow} = \frac{Q \times \omega}{\frac{1}{2}\rho V^3 A}, \quad (1)$$

$$C_t = \frac{T}{\frac{1}{2}\rho V^2 A}, \quad (2)$$

217 and

$$TSR = \frac{\omega R}{V}, \quad (3)$$

218 where  $Q$  is rotor shaft torque in Nm,  $\omega$  shaft revolution speed in rps,  $\rho$   
219 fluid density in  $kg/m^3$ ,  $V$  inflow speed in m/s,  $T$  the thrust/drag in N,  $A$   
220 the rotor sweep area in  $m^2$ , and  $R$  the radius of the rotor, respectively.

221 For the testing measurement, there are three channels captured simulta-  
222 neously for data acquisition, they are: carriage speed, drag/thrust and torque  
223 output. As mentioned previously, the shaft speed channel is separate as an  
224 individual channel that is controlled by the proprietary software. The shaft  
225 revolution speeds in RPM, rounded off from the 2nd decimal point of RPM  
226 (round off error at 1/120 rps), were pre-set on computer for each desired tip  
227 speed ratio. The carriage speeds, thrust and torque coefficients are actually  
228 measured values after applying the gain.

229 The averaged speed, drag/thrust and torque gains obtained are  $g_a =$   
230 0.500, 7.025 and 0.130, respectively and their offsets are nearly zero. There-  
231 fore, the measured value is  $F = V_{measured}(g_a - 0.0)$ .

232 A 32-channel PCI-6254M series data acquisition system by National In-  
233 struments is used. A 32-bit version 2010 Labview was used as the data

234 acquisition software. The computer on the towing tank carriage used is an  
235 HP 8100 Elite Desktop with an Intel Core i5 650@3.2GHz CPU and 8 GB of  
236 RAM, running a 64-bit Win 7.

237 The sample rate for all data points is 1000 Hz which gives about 80 data  
238 points per revolution. For fast propeller testing, a much higher sample rate  
239 at 20 kHz is commonly used in practice but a much lower sample rate can  
240 also be found for wind turbine rotor testing at 20 Hz [3]. The sample rate of  
241 1000 Hz for this testing program was deemed necessary and sufficiently high.  
242 At the beginning of the testing, a sample time of 20 seconds for a carriage  
243 speed of 1 m/s was used but it seemed unnecessarily long. Most of the data  
244 points were obtained using 10 seconds sample time at a carriage speed of 1.5  
245 m/s. There are over 10000 samples over the 10-second period. Only 9500  
246 samples are used to obtain the averaged measurement at each data point.  
247 Using a reduced sample time increased productivity of obtaining 2-3 data  
248 points over one carriage trip of about 80 metres long.

### 249 **3. Results and Discussions**

#### 250 *3.1. Tare thrust and torque to adjust measurements*

251 For turbine rotor performance, accuracy of torque measurement is much  
252 more important than that of drag/thrust, while accuracy on thrust is the  
253 most important for propulsion tests for ship speed estimate. During the  
254 testing the maximum measured torque at a constant 1.5 m/s carriage speed  
255 is about 0.5 Nm and the tare (friction) torque is about 0.1 Nm. The tare  
256 torque relative to the capacity of 4 Nm is too small to eliminate sensitivity  
257 concern. After all the testing was completed, torque sensitivity was care-

258 fully verified and obtained for data correction/adjustment. During the test  
259 at the beginning and the end of each day, tare torques were measured at  
260 various possible shaft rotation speeds without the rotor. No dummy hub was  
261 used. The ITTC propulsion testing guidelines [7] and a wind turbine testing  
262 work [3] were used as reference for tare torque measurement and adjustment.

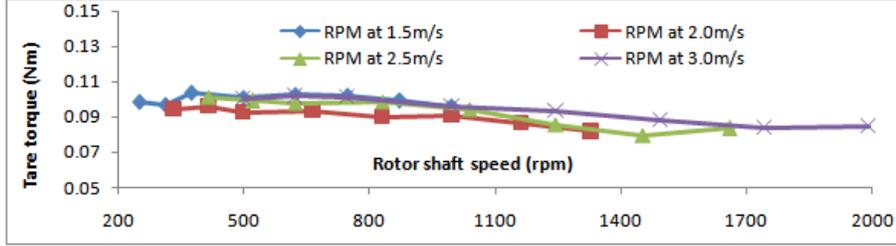
263 A set of extensive tare torque measurement runs were also conducted  
264 to examine tare variations with shaft speeds. Total of four ranges of shaft  
265 speeds were tested corresponding to the inflow speed of 1.5, 2.0, 2.5, and  
266 3.0 m/s. Figure 5 shows the processed measurements. The sample rate and  
267 time were the same as rotor testing condition, i.e., 1000 Hz and 10 seconds,  
268 respectively.

269 Note that measurements shown in Figure 5 were obtained within one day.  
270 For the rotor shaft measured torque adjustment, tare torque values were  
271 obtained each day before the rotor measurement starts and the tare torque  
272 values in the morning were used in the adjustment. Tare torque values were  
273 also obtained after testing at the end of each day and were checked against  
274 these values obtained in the morning. No significant difference was found  
275 so all the measurements were adjusted using the tare torque values in each  
276 morning.

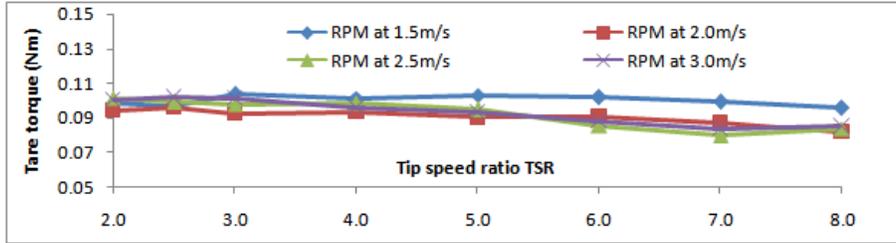
277 For turbine rotor torque measurement, the total rotor shaft torque for  
278 power generation calculation, were obtained by:

$$Q_{adj} = \pm Q_{tare} + Q_{measured} - Q_0, \quad (4)$$

279 where  $Q_{adj}$ ,  $Q_{tare}$ ,  $Q_{measured}$  and  $Q_0$  are adjusted torque measurement, tare  
280 torque, measured torque and torque reading at zero torque load. The sign  
281 of the  $Q_{tare}$  values should be taken to increase the absolute measured torque



(a) Averaged tare torque (Nm) versus rotor shaft speed



(b) Averaged tare torque (Nm) versus equivalent tip speed ratio TSR

Figure 5: Averaged tare torque versus shaft speeds and equivalent tip speed ratios TSR corresponding to an inflow speed of 1.5, 2.0, 2.5 and 3.0 m/s

282 values, for either propulsion (positive torque) or turbine (negative torque)  
 283 mode.

284 For drag measurement, the total rotor shaft drag force for power genera-  
 285 tion calculation, were obtained by:

$$T_{adj} = \pm T_{tare} + T_{measured} - T_0, \quad (5)$$

286 where  $T_{adj}$ ,  $T_{tare}$ ,  $T_{measured}$  and  $T_0$  are adjusted drag/thrust measurement,  
 287 tare drag/thrust, measured drag/thrust and drag/thrust reading at zero  
 288 drag/thrust load. The sign of the  $T_{tare}$  values should be taken to increase  
 289 the absolute measured drag/thrust values for both turbine and propulsion  
 290 mode.

291 *3.2. Test Matrix for Data Acquisition*

292 The two sets of rotor models and the test matrix were designed to pro-  
 293 vide design reference on hydrodynamic performance characteristic of the bi-  
 294 directional tidal turbine rotors and sufficient data for numerical codes val-  
 295 idation. Even though drag measurements are not the most important for  
 296 turbine rotor design, these measurements are very important for numerical  
 297 codes to validate when both drag and torque are available the same time.

298 The initial plan was to obtain thrust and power coefficient for each rotor  
 299 versus a range of tip speed ratio  $TSR$  from 2.0 to 8.0. After a series of  
 300 testing runs, it was found that most power coefficient measured at a  $TSR$   
 301 greater than 6.0 are negative so any power coefficient at  $TSR > 6.0$  is not  
 302 meaningful. Table 3 shows the required shaft speeds corresponding to the  
 303 pre-set  $TSR$  for all the rotors of  $D=0.23$  m, under an inflow speed (carriage  
 speed) of 1.5 m/s.

Table 3:  $TSR$  versus required shaft speed

$TSR$	6.00	5.00	4.00	3.00	2.50	2.00
n (rps)	12.5	10.4	8.3	6.2	5.2	4.2
N (RPM)	747.3	622.8	498.2	373.7	311.4	249.1

304

305 There are total of 6  $TSR$  points and 4 (2 aluminium and 2 nylon) rotors  
 306 so the minimum required number of total data points runs is 24. With the  
 307 calibration runs, tare runs and some trial runs, the number of total runs for  
 308 both first and second phase of the testing program exceeded 300.

309 *3.3. Power and Drag Performance comparison*

310 Figures 6 and 7 show drag and power coefficients of the two set of rotors  
with the same geometry.

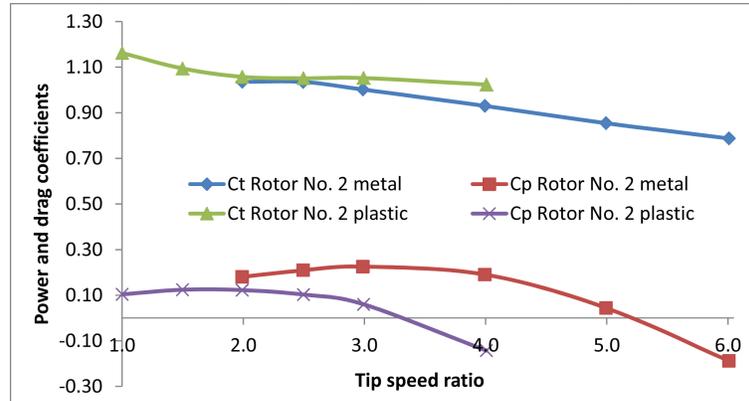


Figure 6: Effect of flexibility and surface roughness on drag and power coefficients, metal versus plastic of Rotor No. 2

311

312 It can be seen for both rotor No. 2 and 3 that the drag coefficient of the  
313 plastic rotors are just slightly higher than the metal rotors throughout the  
314  $TSR$  range, with a slight increase when the inflow speed becomes large at  
315 a tip speed ratio ( $TSR$ ) greater than 2.5. The increased drag of the plastic  
316 rotors is caused by rougher blade surfaces and hence larger skin friction.

317 The maximum power coefficient however, produced by the plastic rotors  
318 is about only 60% of the metal ones. The plastic rotors at a  $TSR$  of greater  
319 than 3.2 (Rotor No. 3) and 3.3 (No. 2) start to produce negative power.  
320 The much reduced power production of the plastic rotors is mainly due to  
321 the flexibility that caused a change in effective angle of attack (or effective  
322 pitch) of the blade sections. It can be seen also that the plastic rotors' cut-in  
323 speed, the minimum inflow speed required to turn the rotor, is much higher

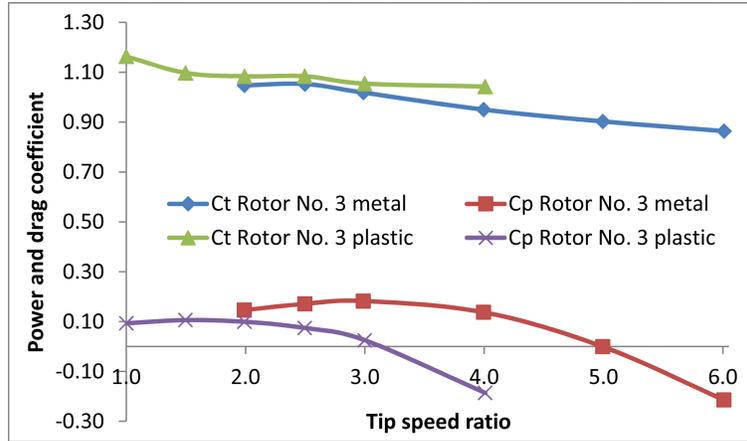


Figure 7: Effect of flexibility and surface roughness on drag and power coefficients of Rotor No. 3

324 than the metal ones —  $TSR$  is proportional to the inverse of the inflow  
 325 velocity. The effect of flexibility on peak power coefficients and cut-in speed,  
 326 is discussed in the following section.

### 327 3.4. Power Performance Analysis

328 The dramatic decrease in power coefficient of the rotor made from plas-  
 329 tic material is caused by flexibility and the change in effective pitch of the  
 330 sections. The substantially increased cut-in speed, i.e., the inability to gen-  
 331 erate power at low speed current becomes significant compared with the  
 332 metal ones: power coefficient falls to zero at  $TSR \sim 3.2$  (Rotor No. 3) and  
 333  $TSR \sim 3.3$  (No. 2) for plastic rotors and  $TSR \sim 5.2$  (Rotor No. 2) and  
 334  $TSR \sim 5.0$  (No. 3) for metal ones, as shown in Figures 6 and 7. However, at  
 335 a very low  $TSR$  of about 1.0 of which the inflow velocity at maximum, the  
 336 plastic rotors can still generate positive power but the metal rotors already  
 337 generate negative power (by extrapolating the power coefficient curves to the

338 left).

339 As mentioned, all the blade sections of the bi-directional rotor are fully  
340 symmetrical. What is the change in pitch, is it increased or decreased, and  
341 how is it changed, due to the flexibility of the plastic material? To find  
342 answers to the above questions, a velocity diagram for a flexible blade section  
343 to determine the effective angle of attack, resulted in a combination of the  
344 blade sectional geometrical pitch, camber, and inflow velocity, similar to a  
rigid foil section presented by Liu [10], is shown in figure 8.

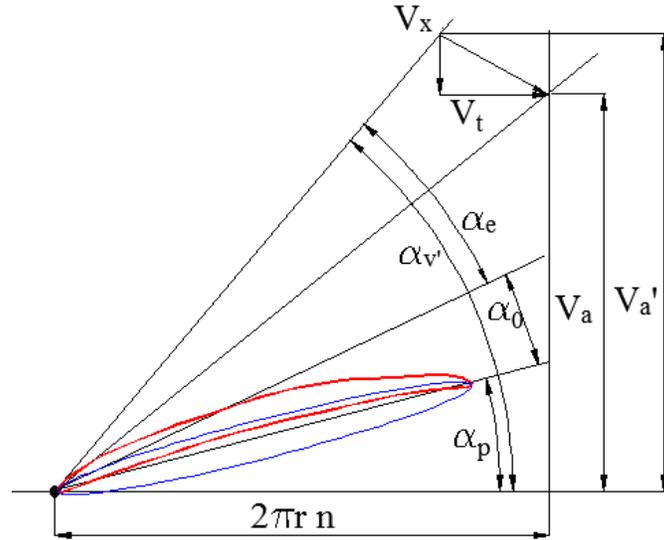


Figure 8: Effective angle of attack velocity diagram of a flexible turbine rotor blade section

345

346 Variables in Figure 8, have been defined in the nomenclature.

347 Due to flexibility, the rigid foil section (in blue) is bent back as it faces the  
348 inflow, similar to a circular arc section (in red). This increases the camber  
349 of the foil section and hence increases the angle of zero lift,  $\alpha_0$ . Normally

350 the higher the flexibility, the larger the deflection. As the foil section is fully  
351 symmetrical, the initial angle of zero lift is zero. The effective angle of attack  
352 of the foil section can be expressed as:

$$\alpha_e = \alpha_{v'} + \alpha_o - \alpha_p \quad (6)$$

353 Equation 6 shows that the larger the negative value of the angle of zero  
354 lift  $\alpha_o$ , the more reduction of the effective angle of attack  $\alpha_e$ . Due to flexi-  
355 bility of the plastic rotors, the more deflection of the blade section the larger  
356 the negative angle of zero lift. Normally for turbine rotors below the stall  
357 region, the lower the pitch, the higher the effective angle of attack (opposite  
358 to a propeller blade section which the higher the pitch the lower the effective  
359 angle of attack), and hence the higher the power coefficient. The only reason  
360 for the plastic rotors to produce an increased power coefficient when effective  
361 angle of attack decreases, is that the reduction in the effective angle of attack  
362 has retarded the severe stall. As is known, stall starts at a sufficiently large  
363 effective angle of attack under a small enough Reynolds number. For exam-  
364 ple, stall occurs at  $\alpha_e > 12^\circ$  for a 2D NACA 0012 foil at a Reynolds number  
365 of about 0.66 million and at  $\alpha_e > 16^\circ$  with a Reynolds number of about 3.18  
366 million [8]. A substantial reduction in power coefficient suggests that at a  
367 very low  $TSR$  of about 1.0, the metal rotor sections are under severe stall  
368 but the plastic rotors still have a power coefficient at the same  $TSR$ . For  
369 turbine testing at constant shaft revolution speed, the lower the  $TSR$ , the  
370 higher the Reynolds number.

371 During phase I of the testing program [13], the effect of Reynolds num-  
372 ber on the inflow speed was discussed and analysed in detail. The power  
373 coefficients for both Phase I and II were obtained at an inflow speed of 1.5

374 m/s for which Reynolds number has little influence on the accuracy of the  
 375 measurement. For these plastic and metal rotors under consideration, at an  
 376 inflow speed of 1.5 m/s, the Reynolds number calculated based on the 0.7R  
 377 chord length, is 0.28 million at  $TSR = 1.0$  and 0.98 million at  $TSR = 6$ .

378 To find out whether the blade sections are under severe stall, let's consider  
 379 the foil tip section at  $r = 1.0R$  at a  $TSR$  of 1.0 and ignore the induced velocity  
 380  $V_x$  and  $V_t$ . Thus the angle of inflow is:

$$\tan(\alpha'_V) = \frac{V'_a}{2\pi nR} = \frac{V'_a}{\pi nD} = \frac{1}{TSR} = 1. \quad (7)$$

$$\alpha'_V = 45^\circ. \quad (8)$$

381

$$\alpha_p = \tan^{-1}\left(\frac{\frac{p}{D}nD}{2\pi nR}\right) = \tan^{-1}\left(\frac{\frac{p}{D}}{\pi}\right), \quad (9)$$

$$\alpha_{p31} = \tan^{-1}\left(\frac{0.31}{\pi}\right) = 5.6^\circ, \quad (10)$$

$$\alpha_{p27} = \tan^{-1}\left(\frac{0.27}{\pi}\right) = 4.9^\circ. \quad (11)$$

382 For the rigid and fully symmetrical blade section, the angle of zero lift of  
 383 metal rotors is zero. The effective angles of attack for the metal rotors no.  
 384 2 and 3 at the blade tip section, assuming a zero chordwise flexibility, are  
 385 then:

$$\alpha_{e27} = \alpha'_{v27} + \alpha_{o27} - \alpha_{p27} = 45 + 0.0 - 4.9 = 40.1^\circ \quad (12)$$

$$\alpha_{e31} = \alpha'_{v31} + \alpha_{o31} - \alpha_{p31} = 45 + 0.0 - 5.6 = 39.4^\circ \quad (13)$$

386 The aspect ratio of a rotor blade is semi infinite if the hub at the blade root is  
 387 assumed an infinitely large wall. At an effective angle of attack of about  $40^\circ$   
 388 at a Reynolds number of 0.28 million, the blade section of the metal rotor

389 with a semi infinite aspect ratio has no doubt a severe stall. A reduction  
390 of the effective angle of attack will then retard or avoid the severe stall and  
391 hence improve the performance of the power generation performance.

392 For the plastic rotors, the angle of zero lift due to the deformation of  
393 the blade section could be estimated approximately using the expression  
394 suggested by Marchaj [16] as:

$$\alpha_o = -360^\circ \left( \frac{f}{c} \right). \quad (14)$$

395 For the soft and flexible blade section of the plastic rotors facing a 1.5  
396 m/s inflow, a bent chord section resulted in a camber of about 20% chord  
397 length, estimated based on the amount of deformation tested in the air by  
398 pressing the blade edges, will result in an angle of zero lift of about  $-23^\circ$  for a  
399 2D foil. The effective angles of attack of the plastic foils are therefore about  
400  $20^\circ$  less than the metal ones, at about  $25^\circ$ . This value of the effective angle  
401 of attack has much less stall than the metals at about  $40^\circ$ . This implies that  
402 a chordwise flexible blade section can reduce the effective angle of attack and  
403 hence retard severe stall, especially at a very large inflow speed when the  
404 rotor encounters a gust current or wind in a harsh environment.

405 The power coefficient of these metal rotors are relatively small (0.22)  
406 because their large solidity of  $EAR = 0.8$  and the bi-directional blade section  
407 (full symmetrical, i.e., zero camber and identical L.E. and T.E. profiles). If  
408 the blade section is designed as a unidirectional profile with a much higher  
409 camber and hence lift, its power coefficient  $C_{pow}$  could be much higher (0.3-  
410 0.4 or even higher). The higher the lift of a wing section, the higher the  
411 pitching moment of the wing. If the same plastic material is used for a rotor  
412 with a high camber profile section and hence a much higher power coefficient

413 around 0.4, the performance reduction due to the very softness and high  
414 flexibility of the plastic material is expected to be similar, unless the plastic  
415 rotor blade section is made much thicker, say, 2 or 3 times as thick.

416 For marine propellers, the angle of zero lift decreases (becomes less nega-  
417 tive) due to the blade chordwise flexibility —blade section bent in an opposite  
418 direction of turbine rotors. This ends up a reduction of the resultant effec-  
419 tive angle of attack at the propeller blade section. Under a very heave load  
420 condition, chordwise deflection becomes large to result in a substantially re-  
421 duced effective angle of attack and hence reduces the possibility of stall and  
422 cavitation. As a result, a flexible propeller blade section will produce a less  
423 thrust production than rigid rotors in medium and light load conditions.

#### 424 **4. Conclusions and Recommendations**

425 Experimental tests were conducted to evaluate the performance of two  
426 sets of metal and plastic bi-directional tidal turbine rotor models. Compari-  
427 son between the metal and plastic rotors hydrodynamic performance in terms  
428 of torque, drag and derived power and drag coefficients were obtained and  
429 are presented. The results show a substantial decrease in maximum power  
430 performance for the plastic rotors — about 40% decrease at a tip speed ratio  
431 of around 3.0 compared with the metal rotors. The plastic rotors operate  
432 in a much smaller *TSR* range and hence a much larger cut-in speed. The  
433 main reason for the reduction in power performance of the plastic rotors was  
434 found to be the change in angle of zero lift because of the bending of the  
435 blade section due to flexibility. The change in zero lift reduces the effective  
436 angle of attack. It is concluded that materials for rotor models with poor

437 rigidity such as polyamide (nylon) produced by selective laser sintering (SLS)  
438 systems, are not suitable for rotor model performance evaluation.

439 The comparison of performance between the metal and nylon rotors indi-  
440 cates that the plastic rotors have a significantly reduced power output (40%  
441 less than the metal ones) mainly due to flexibility of the soft material used.  
442 The flexibility of the chordwise blade section increases the negative value of  
443 the angle of zero lift and hence decreases the effective angle of attack, from  
444 about  $40^\circ$  to about  $25^\circ$  at the tip section at a Reynolds number of 0.28 mil-  
445 lion, as an example estimation. The change in angle of zero of lift due to  
446 flexibility substantially reduced the effective angle of attack has avoided a  
447 severe stall and hence improved the power performance at a very large inflow  
448 speed (very low  $TSR$  of about 1.0).

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## 465 Appendix A. Data in Tables

466 The following are the 4 tables that contain the measurement and analysed  
467 data for the two sets of rotors. Note that the values of drag T in Newtons and  
468 coefficient  $C_t$  should be **doubled** because the drag/thrust gain was tuned to  
469 half, listed in this appendix.

Table A.4: Measurement data for metal rotor No. 2

Rotor No. 2, $P_{D_{07R}}=0.31$ , $P_{D_{tip}}=0.31$ , $EAR=0.80$												
Measured data				Tare Data				Net Outputs				
Run	N (RPM)	$V_{in}$	T (N)	Q (Nm)	T (N)	Q (Nm)	$TSR$	T (N)	Q (Nm)	P (W)	Ct 2	Cp 2
201	249	1.5066	22.63	-0.4023	-1.79	0.0886	1.991	24.42	0.4909	12.805	0.5178	0.1802
201_2	311	1.5035	22.52	-0.3605	-1.78	0.0921	2.494	24.30	0.4526	14.758	0.5175	0.2090
202	374	1.5059	21.82	-0.3140	-1.78	0.0946	2.988	23.60	0.4086	15.989	0.5009	0.2254
202_2	498	1.5023	20.03	-0.1561	-1.77	0.1010	3.994	21.80	0.2571	13.411	0.4650	0.1904
203	623	1.5018	18.25	0.0482	-1.76	0.0957	4.994	20.01	0.0475	3.097	0.4271	0.0440
203_2	747	1.4979	16.61	0.2576	-1.73	0.0899	6.008	18.35	-0.1677	-13.124	0.3936	-0.1880

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Table A.5: Measurement data for metal rotor No. 3

Rotor No. 3, $P_{D_{07R}}=0.27$ , $P_{D_{tip}}=0.27$ , $EAR=0.80$												
Measured data				Tare Data				Net Outputs				
Run	N (RPM)	Vin	T (N)	Q (Nm)	T (N)	Q (Nm)	$TSR$	T (N)	Q (Nm)	P (W)	Ct 3	Cp 3
207	249	1.5058	22.88	-0.3092	-1.79	0.0886	1.992	24.67	0.3978	10.377	0.5238	0.1463
207_2	311	1.5011	22.86	-0.2773	-1.78	0.0921	2.498	24.64	0.3694	12.044	0.5264	0.1714
208	374	1.5059	22.21	-0.2363	-1.78	0.0946	2.988	23.99	0.3309	12.948	0.5092	0.1825
208_2	498	1.5018	20.49	-0.0843	-1.77	0.1010	3.995	22.26	0.1852	9.664	0.4751	0.1374
209	623	1.5016	19.38	0.0963	-1.76	0.0957	4.995	21.14	-0.0006	-0.038	0.4514	-0.0005
209_2	747	1.4971	18.38	0.2811	-1.73	0.0899	6.011	20.12	-0.1912	-14.961	0.4320	-0.2146

Table A.6: Measurement data for plastic rotor No. 2

Rotor No. 2 Plastic, $P_{D_{07R}}=0.31$ , $P_{D_{tip}}=0.31$ , $EAR=0.80$												
Measured data				Tare Data				Net Outputs				
Run	N (RPM)	Vin	T (N)	Q (Nm)	T (N)	Q (Nm)	$TSR$	T (N)	Q (Nm)	P (W)	Ct 2*	Cp 2*
228	125	1.5052	25.54	-0.4644	-1.80	0.0965	1.000	27.35	0.5609	7.342	0.5810	0.1036
228_2	187	1.502	23.83	-0.3487	-1.80	0.0965	1.499	25.63	0.4452	8.718	0.5470	0.1239
226	249	1.5059	23.10	-0.2376	-1.80	0.0949	1.992	24.91	0.3326	8.676	0.5288	0.1223
226_2	311	1.5020	22.83	-0.1237	-1.80	0.0980	2.497	24.64	0.2217	7.230	0.5256	0.1027
227	374	1.5039	22.92	-0.0066	-1.80	0.1020	2.992	24.72	0.1086	4.251	0.5261	0.0602
227_2	498	1.4975	22.04	0.2989	-1.80	0.1078	4.007	23.84	-0.1911	-9.969	0.5117	-0.1429

Table A.7: Measurement data for plastic rotor No. 3

Rotor No. 3 Plastic, $P_{D_{07R}}=0.27$ , $P_{D_{tip}}=0.27$ , $EAR=0.80$												
Measured data				Tare Data				Net Outputs				
Run	N (RPM)	Vin	T (N)	Q (Nm)	T (N)	Q (Nm)	$TSR$	T (N)	Q (Nm)	P (W)	Ct 3*	Cp 3*
229	125	1.5050	25.57	-0.4081	-1.80	0.0965	1.000	27.37	0.5046	6.605	0.5817	0.0933
229_2	187	1.5029	23.94	-0.2856	-1.80	0.0965	1.498	25.74	0.3821	7.482	0.5487	0.1061
230	249	1.5055	23.71	-0.1748	-1.80	0.0949	1.993	25.52	0.2698	7.038	0.5419	0.0993
230_2	311	1.5015	23.58	-0.0628	-1.80	0.0980	2.498	25.38	0.1608	5.244	0.5420	0.0746
231	374	1.5002	22.85	0.0563	-1.80	0.1020	3.000	24.65	0.0457	1.788	0.5272	0.0255
231_2	498	1.497	22.48	0.3561	-1.80	0.1078	4.008	24.28	-0.2483	-12.952	0.5214	-0.1858

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