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### Cognitive modelling of early music reading skill acquisition for piano

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#### Abstract

In the classical music tradition, knowing how to read music is an essential skill and is seen as a fundamental component to develop when learning to play the piano. This research's focus is to study the possible impact of the different teaching approach on the acquisition of initial reading skills. By using cognitive modeling, we are hoping to observe through computer simulation the problem solving and decisionmaking tasks involved in decoding a simple musical score. The paper introduces the Middle-C and Intervallic methods followed by a description of an ACT-R cognitive model and simulation results upon learning with each of the piano methods.

Keywords: Music reading, piano methods, ACT-R.

### Introduction

In the classical music tradition, knowing how to read music is an essential skill and is seen as a fundamental component to develop when learning to play the piano (Galyen, 2005; Sloboda, 2005). However, learning to read musical notation is a long and arduous undertaking (Anderson, 1981; Hahn, 1985) and, despite the value we attribute to it, it is not always successful. In North America and in Europe, piano book tutors are at the centre of a beginner student's learning environment as piano teachers often rely on these books to provide the whole foundation of a pianist's musical education and much of the initial training on reading musical notation (Stewart, Henson, Kampe, Walch, Turner & Frith, 2003; McPherson & Gabrielsson, 2002). However, while having music reading as a common objective, the book tutors have introduced fundamentally different approaches such as the Middle-C, Intervallic or Multi-key approach; and more recently the Eclectic or Modified Multiple Key approach, which has supplanted the original Multi-key (Lomax, 1990). Surprisingly, despite the fact that the main focus of the piano tutors is the development of music reading skills, little is known about how this is done. Piano pedagogy textbooks provide long list of advantages and disadvantages for each of the different teaching approach (Uszler, Gordon & Smith, 2000), however it is all based on intuition and on teachers experience and it has no experimental basis to support the analysis, or formal model of its development. Little scientific information is available to evaluate the real impact of each reading systems, to establish their efficacy and efficiency.

It is well recognized that there is a lack of cognitive models to explain how music reading is acquired. Hodges, the author of the Handbook of Music Psychology (1996) and author of a chapter on music reading in the Handbook of Research in Music Teaching and Learning (1992) wrote that "in music there is no theory devoted specifically to an explanation of music reading: thus, the bulk of the research appears to be devoid of a theoretical underpinning" (1992, p. 469). Sixteen years later, he confirmed that the situation was still the same (Lemay, 2008). The few theoretical models that have been proposed over the years are either still in an embryonic stages or entirely speculative and devoid of an experimental basis (Udtaisuk, 2005). The most well-known cognitive model of music sight-reading was published by Wolf in 1976, and it was developed entirely based on interviews with four pianists (Wolf, 1976). It explains sight-reading as a problem-solving activity of pattern recognition, but no quantitative investigations were undertaken to refine and give legitimacy to the model. Fifteen years ago, Waters, Townsend and Underwood (1998) realized a series of laboratory experimentation to observe how pattern recognition' skills could play an important role in expertise musical sight reading and they have shown that in the pattern-recognition task, immediate recall of presented material correlate strongly with good sight-reading skills. Their study confirmed various experimentations conducted previously by Sloboda (1978, 1985) to show the importance of pattern recognition in various tasks related to music reading. However, while pattern recognition seemed to be a promising avenue to help our understanding of music reading skills, Madell and Hébert (2008) deplore the fact that more recent trends in music reading research has been to experiment with the intricacy of eye tracking technology without a focus on pattern recognition (Kinsgler and Carpenter, 1995). In addition, music reading studies deals with musicians who already know how to read music and have often reach the level of expertise. These models do not always shed lights on the skills required by a novice just being introduced to music notation. Without a solid model of music reading acquisition, it is not surprising that piano teaching material have come to propose very different approaches to music reading.

Piano playing is an elaborate skill that requires the coordination of many cognitive resources and subtle body movements. As such, expert piano playing performance has been the subject of many investigations (Hallam, Cross &

Thaut, 2009; Altenmüller, Wiesendanger & Kesselring, 2006; Parncutt & McPherson, 2002). However, the effect of pedagogical methods on novice performance and learning has not received the same level of attention from a cognitive point of view (McPherson, 2006). Empirical data on the effect of piano methods on learning are scarce, and very difficult to obtained in a controlled setting. As a first step to characterise the effect of pedagogical methods on novice performance and learning, a series of computer simulations were designed. The main objective of the simulations was to compare the resulting states of a common cognitive model after learning to play sequences of short piano pieces from different piano methods. The simulations focused on learning the association between the musical notation and the correct motor movements on the piano keyboard. The task to be performed by the model was a form of sightreading task (Fourie, 2004). The task was to read a note on a music score, and play it on the piano. The model did not intend to capture looking ahead behaviour (Fourie, 2004), the representation and processing of musical sounds (Chikhaoui, Pigot, Beaudoin, Pratte, Bellefeuille & Laudares, 2009), learning motor skills (Jabusch, Alpers, Kopiez, Vauth & Altenmüller, 2009), movement preparation (Palmer, 2005), and multitasking of music reading and motor movements as threaded cognitive tasks (Salvucci & Taatgen, 2008) were excluded from the models.

### The Middle-C and Intervallic approaches

This research's focus is to study the possible impact of the different teaching approaches on the acquisition of initial reading skills. By using cognitive modeling, we are hoping to observe through computer simulation the problem solving and decision-making tasks involved in decoding a simple musical score. We want to examine how the different reading systems impact on the perceptual and motor processes. Since the Middle-C approach and the Intervallic approach have dominated the market for many decades now, we have selected two tutor series that are a good representation of each approach: The A.B.C. of Piano Playing: An Easy Method for Beginners (Berlin, Koniček & Precious, rev. ed. 1983; original ed. 1941); The Music Tree: A Plan for Musical Growth at the Piano (Clark, Goss & Holland, rev. ed. 2000; original ed. 1973; Clark first introduced the intervallic approach under the title Time to Begin in 1955). These authors published their first tutor in the middle of the 20th century, both publications have gone through revision and re-edition and both are still in use by piano teachers. In order to understand the basic characteristics of the reading process involved in each approach, a quick overview of their reading system will be provided.

According to Lomax (1990), the Middle-C reading approach became influential in the early 1900s. Introduced by Mathews in *Standard Graded Course of Studies for the Pianoforte in Ten Grades* (1892), it was then popularised by the very successful tutors written by John Thompson *Teaching Little Fingers to Play* (1936) and the *Modern*  Course for Piano (1936). Berlin's A.B.C. of Piano Playing (1941) published a few years later and selected for our analysis was very much in line with the earlier Middle-C tutors. This reading approach requires the student to place the thumbs of each hand on middle C. The entire first piece is often played with that note only, and then on the following pieces, one note above and one note below middle C are introduced. As new notes are introduced, note names and traditional staff notation are learned simultaneously. The hand position with both thumbs sharing middle C and the other fingers resting on the surrounding white keys is maintained generally for quite a long period of time so that the student becomes familiar with these notes. This reading approach was extremely influential throughout the second half of the 20th century, Schaum and Cupp (1985) wrote that "the Middle C approach continues to prevail because of its unparalleled success and thoroughness. It is probably the most widely accepted keyboard teaching system presently in use" (p. 68) and Lomax (1990) was affirming "the Middle C Method is still one of the most widely used approaches today" (p. 101).

In 1955, Frances Clark revolutionised the way that music reading could be thought with the publication of her Intervallic approach tutor Time to Begin. Elements of this approach had been introduced earlier: partial-staff notation in Loomis' Progressive Music Lessons (Loomis, 1875) and the Landmark approach in Year by Year Books (Williams, 1924). However, Clark was able to define the Intervallic approach like no one had done before her and she popularised it among piano teachers. She developed a reading system where piano students are taught to read music by recognizing intervals. As Uszler (1991) explains "the Intervallic approach stressed the development of spatial-directional reading habits connected with the formation of hand-shapes and movements that follow from intervallic recognition" (p. 107). Students are encouraged to read by contour recognition and the musical staff is introduced one line at a time. They are thought to recognize steps (neighbouring keys) and skips (skipping over one key) on a partial staff, then intervals are introduced (seconds, thirds, fourths, etc.) and finally they are given certain landmarks on the keyboard and they are thought to distinguish the direction of the music through intervals that are related to these guide posts. Unlike the Middle C approach, the Intervallic approach reinforces playing all over the keyboard.

### Simulation of Early Music Reading Skills Acquisition

This section presents the simulation methodology and simulation results obtained by running an initial cognitive model playing a series of musical staves belonging to either the Middle-C or the Intervallic piano methods. The ACT-R cognitive architecture was used to run the simulation (Anderson, Bothell, Byrne, Douglass, Lebiere & Qin, 2004). The simulation procedures consisted of: a) developing an initial cognitive model, b) running the cognitive model with the different conditions represented by the different sequence of music staves from the two piano methods, and c) comparing the model states resulting from the separate simulations.

### Initial cognitive model

The initial model contained only the minimal declarative and procedural knowledge to be able to visually scan a music staff for notes, the piano keyboard for keys, move the hands and fingers over piano keys, press, hold and release them, and the capabilities to process instructions from a tutor. In addition to the content of the declarative and procedural memories described in the following sections, the cognitive model also used base level activation of declarative chunks, production rules compilation, and reinforcement learning.

**Declarative knowledge.** The initial model assumed no prior knowledge of musical notation, and of its association to specific key locations on the piano keyboard. The only declarative knowledge the initial model held were chunks about the association between the number of beats (1 to 4), and the subjective perception of time encoded as ticks. The model however had chunks encoding the approximate duration of 1, 2, 3, and 4 beats (60 beats per minute) using the ACT-R temporal module (Taatgen, van Rijn & Anderson, 2004).

The Figure 1a and 1b presents the visual encoding of the music scores. As figure shows, both the Middle-C and the Intervallic methods share the same encoding, in spite of the differences in the layouts. The visual encoding of a note visual location includes its X and Y absolute visual locations, its relative horizontal and vertical visual locations, as well as four duration encodings using a combination of full or empty circles, with or without stems, and with or without a dot.

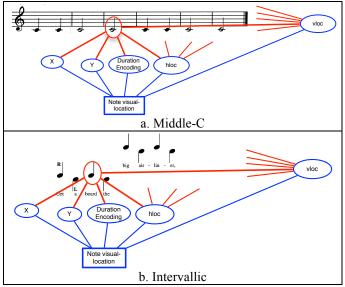


Figure 1: ACT-R visual encoding of music staves.

The Figure 2 presents the visual encoding of the piano keyboard. This encoding is used to direct the hands towards

the proper key to associate with the encoding of the note information on the music staff. The visual encoding of a key location includes the absolute X and Y visual locations, the key color (black or white), the group type (around 2 blacks or 3 blacks), the relative position of a key in the group, as well as the relative position of the group on the keyboard.

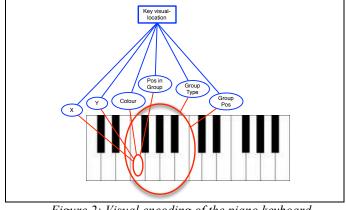


Figure 2: Visual encoding of the piano keyboard using ACT-R chunks.

In addition to the visual encoding of the staves and the keyboard, the model includes a chunk type representing the knowledge about a note, which binds together the musical notation information (staff, vertical location on the staff, duration encoding), motor directives (number of beats, hand, and finger to use), and associated key on the keyboard (group type, group position, key position in group, and key colour). This representation aims at capturing the visual characteristics of notes for musical notations, and in this respect, it differs from a representation of its sound properties (Chikhaoui et al., 2009).

Closely related to the note chunk, the model includes an execution plan. An execution plan is basically a note chunk augmented with the information about the horizontal position of a note on the staff to encode the sequence of notes to play, and the number of ticks (Taatgen et al., 2004) that the note should be pressed. The execution plan acts as the control structure for the model's behaviour. Chunk slots are filled up based on visual encoding and memory retrievals until the plan can be executed. Plan execution chunks are held in the goal buffer of the ACT-R cognitive architecture. The encoding for the note is similar to the theory of event coding where perception and action share a common representation (Hommel, Müsseler, Aschersleben & Prinz, 2001).

**Procedural knowledge** A total of 19 productions are part of the model's initial procedural knowledge. These productions can be classified in productions for processing the tutor's instructions (2), processing the visual information on the staff (2), determining the note duration (5), its key location on the keyboard (4), the finger and hand to use (4), and finally executing the motor action on the keyboard (2). The Figure 5 characterizes the overall flow of control in the model. The first task of the model is to attend the staff and encode the next note visual features. Then the model

attempts to retrieve from declarative memory a note chunk using the visual features as cues. The retrieved note chunk slots are used (or guessed if no note is retrieved) to complete the missing information in the execution plan. The note duration, fingering and key location need to be determined in no particular order. Once the execution plan is completed, the model locates the key on the keyboard, move the hand and finger to the location, and press and hold the key for the given duration.

Figure 3 also includes a description of the flow of control between the student model and an automated tutor. The tutor compares the note to be played by the student model to its performance and provide either a positive reward, or a negative reward with instructions. An instruction consists of a note chunk, correcting the note played. After the reception of an instruction, the model harvests its content to declarative memory, and proceeds to re-attend to same note on the staff. If the note played was correct, the model just proceeds to the next note on the staff.

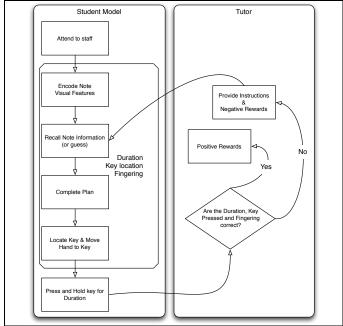


Figure 3: Flow of control and interaction with tutor.

#### **Running the simulation**

The simulation consisted of running a sequence of introductory piano pieces from the Middle-C method, and another one from the Intervallic method. For both sequences, the model started in an identical initial state (described in the previous section). Each sequence had 8 pieces and the model had to play every piece 5 times before moving to the next piece. The following pieces were used in the Middle-C and Intervallic conditions.

Middle-C (Berlin et al., 1983): Second lesson right, Second lesson left, third lesson right, third lesson left, fourth lesson right, fourth lesson left, sixth lesson right, sixth lesson left. Intervallic (Clark et al., 2000): Take Off, Landing, In a Canoe, Space Ship Inchworm, Rock Band, On the Bleachers, Halloween.

After each executed pieces, model states data were collected, in particular the number of declarative chunks in memory, as well as the trace of production rules execution, and their relative utility.

#### **Results and discussion**

There types of data were collected during the simulation execution: the number of declarative chunks in memory, the trace of production rules execution, and their relative utility. The aggregated results are presented in the Figures 4 and 5.

Figure 4 shows the number of declarative chunks in memory as the model progress through the execution of the 40 pieces of music (8 different pieces played 5 times). As the graphic shows, the Middle-C method (lower line) has a very gradual introduction of musical note information when compared to the Intervallic method. The main reason for this difference is somewhat obvious. Because the intervallic method forces the learning musician to play over multiple octaves, the number of note chunks is therefore larger, reflecting the demands of the music scores.

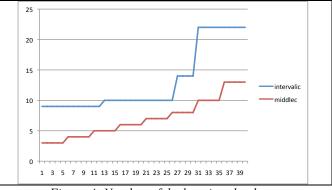


Figure 4: Number of declarative chunks as a function of pieces played.

Figure 5 shows the percent of time spent by the model on building an execution plan, which means the exclusion of the time devoted to visual encoding and motor execution. and the inclusion of processes related to instruction encoding, retrieval, and filling up the execution planning chunk slots. A visual inspection of the graph seems to indicate that the Middle-C method (lower line) requires less retrieval and execution planning time than the Intervallic method. Similar to the previous result on the number of declarative chunks, the larger number of notes to be played with the Intervallic method demands more motor planning. However, the line threads seem to also have different patterns. The Intervallic method has more or less a constant planning time over the course of the simulation. On the other hand, the Middle-C method seems to require an increase of planning time. This increase could be correlated with the increase of notes in the method. The apparent consistency of planning time for the Intervallic method might reflect a ceiling effect cause by the constant number of features per note (location, duration, fingering).



*Figure 5: Percent of time spent on building an execution plan.* 

Results from the production compilation indicated that the model learnt to skip productions, reflecting knowledge acquired about the meaning of the notes. Both methods generated similar productions and their utility values were comparable. For both piano methods, the utility values of new productions were larger than the initial production utilities, in particular for the productions related to the note information associated to the plan duration of a pressed keyboard note.

### Conclusion

Advanced music reading skills (sight-reading) exhibits a smooth coordination of visual encoding and motor skills (Fourie, 2004; Kopiez & Lee, 2008). With skill development, this combination requires a transition from multitasking to cognitive processes concurrency. As notes are being read on the staff, motor movements are planned and executed, while the reading process is progressing beyond what is currently played. Sight-reading efficiency demands the coordination of psycho-motor speed, early acquired expertise, mental speed, and the ability for auditory imagery (Kopiez & Lee, 2008).

As an initial step towards characterizing the effect of different piano methods on the acquisition of piano playing skills, we constructed a minimal cognitive model which acquired declarative and procedural knowledge through the execution of novice piano pieces form the Middle-C and Intervallic methods. Inspection of the resulting models revealed differences in terms of declarative memory and cognitive processing demands. In particular, the intervallic method requires a larger number of declarative knowledge related to notes, and more gesture planning than the Middle-C method.

There are some limitations to the current state of the research that need to be mentioned. In particular the model would need to integrate a representation of sound to a note (Chikhaoui et al., 2009). This is important because the inner playing of a piece of music is a good determinant of music reading performance (Fourie, 2004). Also the model only focuses on individual note and has no notion of musical phrase. A more realistic model of motor movement could also be added, but mostly the model should be able to adress the visual and motor concurrency and the development of reading ahead strategies. The model does not aim at

modelling errors. For example Fourie (2004) reports that 80% of error in sight-reading are rhythmic in nature, probably caused by the difficulty related to locating the correct key on the keyboard. This measure could be an interesting one in comparing the Middle-C and Intervallic methods, given the larger number of keyboard keys in the latter method. In this respect, the model should also have a representation of intervals, which as the moment is not present. Note accents were left out of the simulation, even though it is present in the introductory pieces of both the Middle-C and Intervallic methods.

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