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SORPTION AND LENGTH - CHANGE SCANNING ISOTHERMS OF METHANOL AND WATER ON HYDRATED PORTLAND CEMENT

BY

ROLF F. FELDMAN

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ISOTHERMES DE SORPTION ET DE VARIATION DIMENSIONNELLE DU METHANOL ET DE L'EAU SUR LE CIMENT PORTLAND HYDRATE

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SOMMAIRE

Le but de cette recherche était d'examiner la nature et la réversibilité des isothermes CH₂OH et H₂O et de comparer leurs caractéristiques de sorption et de variations dimensionnelles. A cause de plusieurs facteurs distinctifs des isothermes, ces caractéristiques pour l'eau sur le ciment portland hydraté ont causé quelques controverses en ce qui touche les propriétés des surfaces, la stoechiométrie des composés et les mécanismes de variations dimensionnelles et de fluage.

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Supplementary Paper III-23 Sorption and Length-Change Scanning Isotherms of Methanol and Water on Hydrated Portland Cement

Rolf F. Feldman*

Synopsis

The purpose of this work was to investigate the nature and the reversibility of the CH_3OH and H_2O isotherms, and to compare their length-change and sorption characteristics. These characteristics for water on hydrated portland cement have caused some controversy, due to several complicating features in the isotherm, with regard to the surface properties and stoichiometry of the compounds, and the length change and creep mechanisms.

Introduction

The development of the present model of hydrated portland cement has been largely based on surface chemical considerations; this involved establishing criteria for distinguishing between chemical and physio-sorbed water. The determination of the stoichiometry of the tobermorite gel, its water surface area, and its porosity was based on these criteria, and these parameters are among the most important factors related to the phenomena of expansion-contraction and creep, and the mechanical properties, strength and elasticity.

The most important experiments performed using the surface chemical approach have been the sorption and length change isotherms but, as no detailed investigation of the isotherms has been made, their validity and results obtained from them have been assumed to be correct. Results of surface area investigations, however, differ markedly from those obtained from nitrogen adsorption, and this has led to some suspicion of the results.

In a series of papers by the author and co-workers, (1, 2) a more detailed examination of the isotherms

was started, involving both length change and weight change as function of the vapour-pressure of water; measurements of Young's modulus and relative breaking stress were also made as functions of vapour pressure. The results led the authors to conclude that the surface area of hydrated portland cement was considerably lower than the accepted value ($\simeq 200$ m²/gm), and that inter-layer hydrate water was playing a role in both the length change and sorption isotherms, and in the variation of Young's modulus with relative humidity.

The present work is a further stage in these investigations. Detailed cycling and scanning loops were obtained for samples dried at three different conditions during the determination of precise length change and weight change isotherms based on numerous data for water and methanol on bottle and pastehydrated cement.

Results qualitatively confirmed the earlier work, although some assumptions made previously were proved to be not completely correct. The work enabled a revised model for portland cement paste to be made, however, and allowed further evolution of the theory of volume change and suggestions with regard to the creep phenomena.

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^{*}Division of Building Research, National Research Council of Canada, Ottawa, Canada

Experimental

Meterials

The cement used in this work was a type I; its composition was reported in a previous paper (1). The cement was hydrated in two ways; paste hydrated for 1 year at a water cement ratio (w/c) of 0.5 and bottle hydrated for a period of 4 months at a w/cratio of 5.0. The degree of hydration and other properties are shown in Table 1. The bottle-hydrated cement was stored and conditioned in desiccators to 10 to 15 per cent relative humidity (R. H.) using a concentrated NaOH solution. The cast paste cylinders were sliced to 0.05 in. (1.27 mm) thickness and were approximately 1.25 in. in diameter and then stored as above. Compacts were formed at a load of 10,000 lb in a mould 1.25 in. (3.175 cm) diameter from the bottle-hydrated cement. The procedure for making the compacts and the samples has been described previously (2).

The methanol used in this work was purified by making a magnesium iodine Grignard complex by refluxing magnesium turnings and iodine in a large excess of 99 per cent pure methanol. After several distillations, the methanol was distilled directly into the high-vacuum apparatus.

Apparatus

The high-vacuum apparatus used for this work was designed to expose 12 samples simultaneously for long periods to the same vapour pressure conditions, with air excluded. Six of these samples were mounted in individual tubes on quartz spirals of the McBain-Bakr type and gave values of the weight changes to a sensitivity of 3.0×10^{-5} gm. The remaining six samples were mounted on modified Tuckerman optical exten-

someters and placed in individual cells equipped with optical windows (3). This determined the dimensional changes to a sensitivity of 4×10^{-6} in./in. A quartz Bourdon-type spiral gauge was used to measure the vapour pressure to a sensitivity of 1 micron and an absolute accuracy of 10 microns at low pressures.

A three-stage oil diffusion pump backed by a rotary vacuum pump was used to obtain pressures of 10^{-6} mm of mercury. The adsorbate was introduced into the system from a bulb immersed in a bath that could be controlled at temperatures down to -45° C within 0.05°C, although most of the pressure readings were taken with the Bourdon gauge. The samples were maintained at 21.3°C within 0.05°C by immersing the lower ends of the tubes and cells containing the samples to a depth of 12 in. in a controlled bath. Room temperature was controlled at 23°C \pm 0.5.

Procedure

Two samples measuring 3 by 1 by 0.127 cm were cut from the discs and mounted, one section on the extensometer and the other on the quartz spiral. Samples were degassed by evacuating simultaneously through a manifold. The samples were heated during the evacuation. Three samples of bottle hydrated cement were used and one each was heated at: 80°C for 3 hours, 85°C for 3 hours, and 95°C for 3 hours plus 1 hour at 96°C. Two samples of hydrated paste were used and one each was heated at: 85°C for 3 hours, and 95°C for 3 hours plus 1 hour at 96°C. Preliminary work using a vacuum electro-balance and thermal balance techniques had established that vacuum degassing at 85°C for 3 hours with these samples produced the same result for the non-evaporable water as the conventional 'd-drying' procedure. For

| | Non-evaporable water | | Nitrogen surface area, m²/g, 85°C | | Methanol area | | Conventional water area | | | | | |
|-----------------------------------|----------------------|---|--------------------------------------|-------------------------------|------------------|-------------------|-------------------------|-------------------------------------|------------|-----|------------|------------|
| | Wn | (Wn/25) × 100 | Measured (a) | For complete hydration (b) | (a) | (b) | 80° | (a) 85° | 96° | 80° | (b) 85° | 96° |
| Bottle hydrated Paste hydrated | 21.5 23,0 | 86 92 | 30 47 | 35 51 | 37 | 43 | 130 | 142 152 | 150 147 | 151 | 165 165 | 174 160 |
| | | (ΔL/L)/(, | ∆W/W) Values | for bottle-hydrate | d cement o | degassed at | 80°C. | | | | | |
| | | | On desorption | | | | | Separation of adsorption-desorption | | | | |
| | Tot | al Ro | eversible | Before datum point | | After datum point | | curves at P/P ₀ of 0.10 | | | | |
| Water Methanol | | 0.0770 0.0220 0.0640 0.0525 (estimate) | | | 0.0860 | | 0.0375 0.0955 | | | | | |

Table 1. Some sorption properties of the hydrated portland cement samples

the methanol isotherm, 1 day was generally allowed for equilibrium between points; for the water isotherm from 1 day to as much as 33 days was allowed. Generally 1 to 3 days was found adequate. It took over 10 months to determine the whole isotherm. Adsorption was effected by allowing the manifold and samples

to attain the desired vapour pressure by control of the temperature of the bath in which the adsorbate source was immersed, or by introducing or withdrawing adsorbate from the manifold and system and measuring the vapour pressure. It was found that equilibrium was attained more rapidly with the latter method.

Theory

thus

Adsorption

The isotherm for a given solid gas system should be reversible if there is no irreversible change in the nature of the solid and/or gas, since there thus can be only one equilibrium state at a given vapour pressure. This is usually the case at low pressures but at high pressures the problem of primary hysteresis arises. This is usually related to the pore structure of the solid and a change in nature of the adsorbate.

The well-known B. E. T. equation, valid for the low pressure region, implicitly assumes reversibility and a constant surface area. There is an isotherm, however, referred to as Type C, which has the characteristic that the ascending and descending branches only join at very low or zero pressure(4). Type C loops are found with some graphites, clay minerals, and hydrated portland cement (1). This low-pressure hysteresis phenomenon is usually attributed to irreversible intercalation of adsorbate within the structure of the solid, which usually has a layer structure. Changes in the spacing of some of these layers has been observed (5) by X-ray methods, but unfortunately, due to the disordered nature of the layers of the hydrated silicates in hydrated portland cement, this has not been possible for this material.

Length Change due to Adsorption

The Gibbs' adsorption equation is extremely important in length-change adsorption theory (6), but it has been applied in different ways by various workers and sometimes not justifiably. The equation

$$\Delta F = -RT \int_{0}^{P} n \frac{dP}{P}$$
 (1)

represents the change in free energy of pure adsorbent from its initial state under its own vapour pressure to its combining state, provided that this integral represents a path of thermodynamic reversibility. nis the number of moles of adsorbate on a fixed mass of absorbent. If it is supposed that the constant solid surface area, $\sigma m^2/g$, has undergone a change in surface tension, Δy , one can write

$$\Delta F = \sigma \Delta \gamma \tag{2}$$

$$\Delta \gamma = \frac{\mathrm{RT}}{\sigma} \int_{0}^{\mathrm{P}} n \frac{d\mathrm{P}}{\mathrm{P}}$$
(3)

 $\Delta \gamma$ in fact indicates changes in the state of stress of the solid brought about by the interaction of the adsorbed molecule with forces on the solid surface; these forces have placed the solid in a state of compressive stress.

The Bangham equation (7) provides a basis for testing Gibbs' equation on solids

$$\frac{\Delta L}{L} = k_1 \Delta \gamma \tag{4}$$

where $\Delta L/L$ is the length change of an adsorbent during the reversible adsorption process. From another relation derived by Bangham and co-workers (7), the Young's modulus of the solid material may be calculated:

$$\mathbf{E} = \boldsymbol{\rho} \frac{\boldsymbol{\sigma}}{k_1} \tag{5}$$

where E is Young's modulus of the material, and, ρ , in g/cc, is the density. The equation is derived for plates, or infinitely long cylinders, where the only surface is that of the curved surface of the cylinder or the major surface of a thin plate. The latter model might approximate hydrated cement paste. As Gibb's equation requires thermodynamic reversibility it can only be used at low pressures where normal hysteresis does not occur. If low pressure hysteresis does occur, then this region of the isotherm may be also irreversible. As will be shown later, this is true for hydrated portland cement, but a way has been found to overcome it.

Some authors (8, 9, 10) have used an equation of the osmotic pressure type and applied it to the low pressure region:

$$\Delta \mathbf{P} = \frac{\mathbf{RT}}{\rho \mathbf{M}} \ln \frac{\mathbf{P}_2}{\mathbf{P}_1} \quad \text{or} \quad \frac{\Delta \mathbf{L}}{\mathbf{L}} = k_2 \frac{\mathbf{RT}}{\rho \mathbf{M}} \ln \frac{\mathbf{P}_2}{\mathbf{P}_1} \quad (6)$$

where ΔP is suggested as being the pressure of the adsorbed film. This equation can only be valid if the water-hydrated cement system is considered to be a dilute solution, i.e., a change in concentration of water with respect to the adsorbent is not taking place during adsorption or desorption, and if the adsorbed water is not adsorbed water but bulk water. Both of these assumptions are completely untenable in this region.

In the reversible high-pressure region of the isotherm where capillary condensation has occurred and menisci exist, one might assume that a change in concentration is not taking place, if one defines capillary water as being remote from the surface forces; thus the capillary water in this assumption will also be 'bulk'. The capillary water maintains equilibrium with different vapour pressures by changing the radius of its meniscus. The water within the range of surface forces, however, will still effect a change in surface free energy with a change in vapour pressure of the system even if one defines it as being constant at two molecular layers. This must be taken into account as in the equations for the capillary region:

 $\Delta \gamma = \frac{\mathrm{RT}}{\sigma} \cdot n \int_{\mathrm{P}_1}^{\mathrm{P}_2} \frac{d\mathrm{P}}{\mathrm{P}}$

and

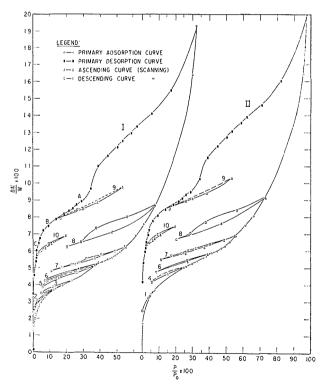
$$\frac{\Delta L}{L} = \left(k_1 \frac{RT}{\sigma} \cdot n + k_2 \frac{RT}{\rho M}\right) ln \frac{P_2}{P_1}$$
(7)

Results and Discussion

Water Adsorption

The sorption and Length Change Isotherms

The sorption and length change isotherms for the bottle-hydrated cement degassed at 80°C and 96°C are shown in Figs. 1 and 2 respectively. Results for a



degassing temperature of 85°C were also obtained, but are not presented here. They were of a similar nature, but gave a slightly different 'conventional water surface area, as is shown in Table 1. In addition, it was observed that the weight of water present (in per cent) on the descending boundary curves of the isotherm at P/P₀ of 0.14, for the three temperatures 96°, 85° and 80°C, was 8.51, 8.19 and 7.91 per cent respectively. These values were less than 0.5 per cent different from the weight lost on degassing. As the starting condition was only known approximately

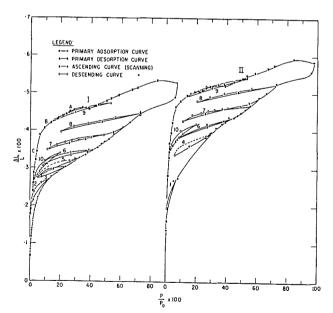


Fig. 1. Weight change isotherms for bottle-hydrated portland cement compacts: I—degassed at 80°C; II—degassed at 96°C (scanning loops marked 1 to 10).

Fig. 2. Length change isotherms for bottle-hydrated portland cement compacts: I—degassed at 80°C; II—degassed at 96°C (scanning loops marked 1 to 10).

 $(P/P_0 \text{ of } 0.10 \text{ to } 0.15)$, it must be assumed that practically all the water lost on degassing was regained after the sample had been returned to the starting condition through the P/P_0 of 0.97. The degassing procedure, however, produced an irreversible shrinkage.

A general examination of both length and weight change in the two isotherms shows a large low pressure hysteresis formed by what will be called the adsorption (ascending) and desorption (descending) boundary or primary curves. Off the boundary curves are scanning loops, which contain descending and ascending portions. These loops are numbered on Figs. 1 and 2 from 1 to 10, and will be referred to as loop 1, 2, etc. It will be observed that the point where the scanning loop left the primary curve was always very close to, if not exactly at, the point where it rejoined the primary curve. This is considered as evidence for good equilibrium. The scanning loops determined for the two isotherms in Figs. 1 and 2 were not the same in all cases; detailed analysis of only the sample degassed at 80°C will be made here, however, and passing reference to the others included.

All the experimental points obtained for this sample are shown in Table 2, in the order in which

they were obtained. The points with asterisks are those which have left the primary curves and are of scanning loops, both descending and ascending.

Length and sorption isotherms for one of the pastehydrated samples, the one that was degassed at 85°C, are shown on Fig. 3. Again the similarity with the other samples is striking, although the extent of the low pressure hysteresis is not as great as for the paste samples. The general form of the primary curves for the paste- and bottle-hydrated samples agrees with that obtained from somewhat fewer data obtained by the authors and co-workers in a previous study (11), but the low-pressure hysteresis here is much larger than was obtained in an earlier investigation (1). It will be shown that this is due to the more severe drying used in the present study. No detailed analysis will be made here of the paste samples (Fig. 3), but it was again found that all the water lost on degassing was regained after the sample had been returned to the starting condition through the P/P_0 of 0.97; the surface areas for water and nitrogen are given in Table I. The areas, corrected for incomplete hydration, vary from 151 to 174 m²/g for the water determination, and are only a bit lower than usually obtained, but,

| $P/P_0 \times 100$ | $\Delta W/W \times 100$ | ${\Delta L/L} \times 100$ | T, days | $rac{P/P_0}{	imes 100}$ | $\Delta W/W \times 100$ | $rac{\Delta L/L}{	imes$ 100 | T, days | $	extsf{P/P_0} 	imes 100$ | $\Delta W/W \times 100$ | $rac{\Delta L/L}{	imes$ 100 | T. days |
|--------------------|-------------------------|---------------------------|------------|--------------------------|-------------------------|------------------------------|---------------------|---------------------------|-------------------------|------------------------------|------------|
| Sorption | | | | | Sorption (C | Cont'd) | Desorption (Cont'd) | | | | |
| 0.27 | 1.27 | .0844 | 6 | 8.21* | 4,25 | ,3068 | 2 | 62.01 | 13.41 | | 1 |
| 0.44 | 1.42 | .0972 | 2 | 27.02* | 4.94 | .3352 | 2 | 58.51 | 13.02 | .4940 | 1 |
| 0.59 | 1.58 | .1108 | 3 | 38.72* | 5.29 | .3484 | 1.5 | 53.41 | 12.54 | .4860 | 1 |
| 0.79 | 1.69 | .1196 | 2 | 44.68 | 5.54 | .3552 | 2 | 50.40 | 12.17 | .4788 | 1 |
| 1,06 | 1.94 | .1336 | 2 | 47.17 | 5.64 | .3648 | 2 | 44.76 | 11.65 | .4692 | 1 |
| 1.49 | 2.06 | .1440 | 3 | 49.38 | 5.75 | .3700 | 2 | 38.87 | 11.04 | .4572 | 1 |
| 2.22 | 2.28 | .1584 | 1 | 52.03 | 5.93 | .3792 | 3 | 34.48 | 9.71 | .4612 | 1 |
| 3.08 | 2.60 | .1860 | 7 | 55.38 | 6.21 | .3900 | 3 | 28.99 | 8.94 | .4540 | 1 |
| 4,37 | 2.84 | .2052 | 7 | 48.57* | 6.04 | .3884 | 2 | 26,14 | 8.77 | .4500 | 1 |
| 5.44 | 3.08 | .2220 | 7 | 40.46* | 5.80 | .3836 | 2 2 | 23.93 | 8.54 | .4444 | 1 |
| 7.42 | 3.24 | .2392 | 8 | 31.82* | 5.58 | .3772 | 1 | 21.38 | 8.35 | .4396 | 1 |
| 12.31 | 3.70 | .2688 | 8 | 27.53* | 5.35 | .3732 | 3 | 18.52 | 8.21 | .4340 | 1 |
| 7.24* | 3.44 | .2608 | 11 | 23,10* | 5.24 | .3684 | 1.5 | 13.94 | 7.91 | .4220 | 1 |
| 2.63* | 3.07 | .2384 | 8.5 | 17.48* | 5.06 | .3612 | 1 | 29.89* | 8.51 | .4472 | 1 |
| 0.84* | 2.65 | .2068 | 7.5 | 11.05* | 4.85 | .3484 | 2 | 38,35* | 8,88 | .4588 | 1 |
| 0.36* | 2,36 | .1780 | 13 | 25.91* | 5.25 | .3668 | 3 | 53.23* | 9.78 | .4740 | 1 |
| 2,42* | 2.86 | .2152 | 6 | 36.75* | 5.59 | .3780 | 2 | 26.37* | 8.45 | .4476 | 1 |
| 13.92 | 3.76 | .2772 | 15 | 54.74* | 6.32 | .3956 | 2 | 16.32* | 7.96 | .4284 | 1 |
| 17.68 | 3,96 | .2876 | 2 | 61.20 | 6.94 | .4088 | 3 | 9.47 | 7.49 | ,4060 | 1 |
| 23.35 | 4.26 | .3068 | 6.5 | 66.20 | 7.62 | ,4228 | 3 | 6.38 | 7,24 | .3880 | 1 |
| 12,18* | 3.85 | .2952 | 6 | 72.70 | 8.75 | .4452 | 3 | 4,43 | 6.75 | .3448 | 1 |
| 5,14* | 3.50 | .2736 | 5 | 56,19* | 8.05 | .4340 | 2 | 3.58 | 6.49 | .3228 | 1 |
| 7.90* | 3.56 | .2744 | 33 | 38.07* | 7.35 | .4180 | 2 | 2.32 | 6.05 | .2880 | 1 |
| 31.00 | <u> </u> | .3240 | 1 | 28.66* | 6.56 | .4100 | 2 2 | 2.21 | 5.62 | .2600 | 1 |
| 38.00 | 5,23 | .5240 | 1 | 20.44* | 6.26 | .3972 | 2 | 4,17* | 5.87 | .2780 | 1 |
| 5.92* | 3.87 | .2760 | 3 | 47.29* | 7.13 | ,4248 | 2 | 6,48* | 6.09 | .2896 | 1 |
| 15.30* | 4.38 | .2972 | 3.5 | 72,79 | 8.73 | .4484 | 2 | 7.38* | 6.14 | .2952 | 1 |
| 26.38* | 4.73 | .3160 | 2 | 95.25 | 16.42 | .4884 | 2 3 | 11.15* | 6.41 | .3116 | 1 |
| 29.95* | 4.87 | .3228 | 1 | 96.98 | 19.31 | .5276 | ī | 19.64* | 6.92 | .3392 | 1 |
| 32.80* | 4.87 | .3284 | | 20.20 | Desorp | | - | 9.66* | 6.41 | .3180 | 1 |
| 36.80* | 4,98 | .3264 | 2 2 | 84.01 | | .5340 | 2 | 1.89 | 5.36 | .2396 | 1 |
| 38.00* | 5.18 | .3428 | 2 | 82.03 | 15.51 | | 2 | 0.93 | 4.59 | .1900 | 1 |
| 41.45 | 5.20 | .3420 | 2 | 70.86 | 14.16 | .5156 | ī | 0.42 | 3.45 | .0648 | 1 |
| 26,88* | 5.38 4.95 | .3400 | 2 2 | 67.33 | | .5096 | i | 0.005 | 0.07 | -0.420 | 2 |

Table 2. Length change and weight change isotherms for the sample of
bottle-hydrated cement degassed at $80^{\circ}C$

*Points on scanning curve

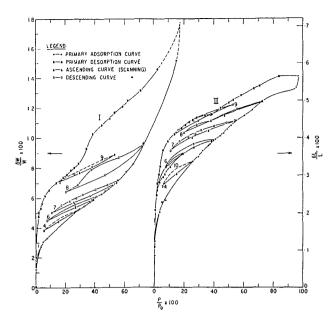


Fig. 3. Weight change (I) and length change (II) isotherms of hydrated portland cement paste (water/cement ratio = 0.5). Scanning loops marked.

as will be shown, a water area determination cannot be considered as a valid procedure. The nitrogen areas are, for these samples, 1/3 to 1/5 of the water areas, as has been observed by other workers (12).

Detailed examination of the isotherms, and especially the loops (Figs. 1 and 2), reveal the following:

(a) The isotherm is irreversible even at as low a P/P_0 value as 0.05 as is shown by loop 1; much of the irreversibly sorbed water, contributing to the low-pressure hysteresis, is sorbed below a P/P_0 of 0.35. (This irreversibly sorbed water, as will be shown, is interlayer hydrate water and will also be referred to as 'irreversible water.')

(b) All descending portions of loops 3 to 9 are essentially parallel and are much less steep than the primary curve. Thus means of course that a large part of the water sorbed on the primary adsorption curve is irreversible.

(c) In loops 7 and 8, where the descending curve has not gone below a P/P_0 of 0.11, the loops, although very close to, are not quite reversible.

(d) Both loops 7 and 8 exhibit a small primary hysteresis. This is to be expected since these loops leave the primary curve at P/P_0 values of 0.56 and 0.73 respectively. The desorption of the capillary water takes place between P/P_0 values of 0.38 and 0.29. This is lower than has been reported (8), but is confirmation of what was found previously (1).

(e) The primary desorption curve shows a large

primary hysteresis. This primary hysteresis disappears between P/P_0 values of 0.39 and 0.29. The length change isotherm shows a small expansion in this region.

(f) The primary desorption curve below a P/P_0 of 0.29 shows that the low pressure hysteresis has increased markedly since the last loop, 8; the length change isotherm shows large changes between earlier loops, but does not show a further change in this region in the same relation to the irreverible water added.

(g) Fig. 3 shows the $\Delta L/L$ vs. $\Delta W/W$ plots for the sample degassed at 80°C; loops are numbered. Curve I contains most of the loops, curve II is a magnified version of I, and curve III shows only the primary ascending and descending curves. The $\Delta L/L$ vs. $\Delta W/W$ characteristics for the primary curve and the loops are completely different; the slope of the primary curve is much steeper and only if the loop goes below a P/P_0 value of 0.10 or thereabout does it become steep. This implies that the mean location of the water sorbed on the primary loop is different from that desorbed. The water sorbed on the primary curve is composed of a reversible and irreversible component and the $\Delta L/L$ vs. $\Delta W/W$ slope of this water is much greater in the low pressure range than the reversible component, most of which comes off separately if the loop is not carried to too low a pressure. It now seems clear that this 'irreversible water' is interlayer hydrate water. Sorption and length change theory (13) (see also earlier part of this paper) allows for length change due to physical adsorption by a decrease in surface energy of the solid. If a "crystal" is anisotropic, this may lead to the development of shear forces. In the case of hydrated cement, the hydrated silicate which has lost most of its intelayer hydrate water will accept physically adsorbed water (sometimes referred to as "reversible water") on its external surface, most of which is perpendicular to the *c*-axis. The resulting expansion on top of the layer should cause some warp at the edges, allowing some interlayer hydrate water to enter. This process will continue up the isotherm. (More will be said later about how this interlayer water enters and leaves and how it affects $\Delta L/L$ and Young's modulus.)

(h) The primary desorption curve below P/P_0 of 0.29, (Figs. 1 and 2) is surprisingly much steeper than all the desorption curves of the scanning loops. Loop 9 shows that 'irreversible water' was being desorbed in this region; the $\Delta L/L$ vs. $\Delta W/W$ slope (Fig. 4) for the primary desorption loop is much lower than in the primary adsorption region. Loop 9, however, is still steeper than loop 7, and it appears that some

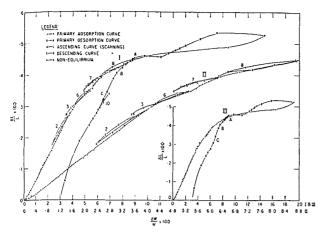


Fig. 4. $\Delta L/L$ vs. $\Delta W/W$ plot for water sorbed on bottle-hydrated sample degassed at 80°C: I—containing all loops; II—enlarged portion of I; III—only showing primary sorption and desorption curves (scanning loops marked 1 to 10).

interlayer hydration may be taking place along the adsorption curve of loop 9.

(i) ABC on Figs. 1, 2 and 4 mark the area where two regions of distinctly different slope of the $\Delta L/L$ vs. $\Delta W/W$ curve occurs on the primary desorption curve (2). As will be seen later, this probably represents a change in the response of length change due to unit weight loss of interlayer water. The assumption made previously (2) that this characteristic is constant now appears to be incorrect.

(j) The line BC marks the region where a considerable hysteresis in the $\Delta L/L$ vs. $\Delta W/W$ plot is formed (Fig. 4). (How this may illustrate the difference between entry and exit of interlayer water will be diccussed later.) Below BC, the curve first gradually returns towards the zero point but then turns away, resulting in a large contraction below the zero point at zero $\Delta W/W$.

(k) Loop 10 illustrates how a smaller low pressure hysteresis may be obtained in the isotherm when the sample has not been degassed as much as the initial degassing. Along the adsorption curve of the loop, a change in slope again occurs at about a P/P_0 of 0.10.

(l) Sorption and desorption measurements were taken at very low pressures (Table 2). On sorption the lowest P/P_0 value was 0.0027 and 0.0044 gave a $\Delta W/W \times 100$ value of 1.42. On desorption, the value was 3.45 at a P/P_0 value of 0.0042. This shows that there is large hysteresis in the sorption isotherm even at the lowest pressures. The length change isotherm shows a hysteresis in the other direction. At P/P_0 below 0.0093, a very large shrinkage occurs (0.420 per cent below the original zero). The pressure at zero

was less than 1 micron of Hg (10⁻³ torr).

Construction of a Reversible Isotherm

The following conclusions can be derived from the previous discussion.

(a) The water isotherm for the several degrees of drying investigated is irreversible at all primary regions and, as such, cannot be used for B. E. T. calculations.

(b) As a large but unknown portion of the 'sorbed' water in the low pressure region is interlayer hydration, the surface area must be considerably lower than the original value calculated for water. The surface area obtained from N_2 will be considered here as the more reliable figure.

It still seems possible to separate, to some extent, the interlayer and physically adsorbed water from the isotherm. This can be done with the help of the scanning loops. If the desorption part of each loop up to the point where it overlaps with the inception of the previous loop (at a lower pressure) is regarded as reversible and involving only physically held water, one would be able to calculate for the pressure region over which the loop extended, the amounts of 'irreversible' and 'reversible' water sorbed along the primary adsorption curve. Since loops 7 and 8 exhibited primary hysteresis, the adsorption curve was used in these instances. For the estimate between P/P_0 of 0.727 and 0.97, it was assumed that no 'irreversible water' was desorbed between P/P_0 of 0.97 and 0.289; then the separation between this point on the primary desorption curve and loop 8, represented the water irreversibly sorbed between P/P_0 of 0.727 and 0.97. This procedure was also performed for the length change isotherm.

Fig. 5 shows the reversible length change and sorption isotherms. The desorption curve between P/P_0 of 0.97 and 0.289 was fitted on this curve. From the length change isotherm it is clear that too much contraction took place in this region to fit properly onto the adsorption curve. It is suspected that some 'irreversible water' was lost between at least P/P_0 of 0.345 and 0.289. Calculation of the reversible desorption between P/P_0 of 0.289 and 0.139 using loop 9 was not satisfactory since the validity of the assumption that the adsorption curve of the loop only involves physical water is suspect.

A plot of $\Delta L/L$ vs. $\Delta W/W$ (Fig. 5), shows a sharp deviation from the linear part of the curve at a P/P₀ of 0.10. This linear plot has been observed for the adsorption of water on porous glass, finely divided silica, precipitated calcium carbonate, calcium sulphate hemihydrate and Ca(OH)₂ and goes through

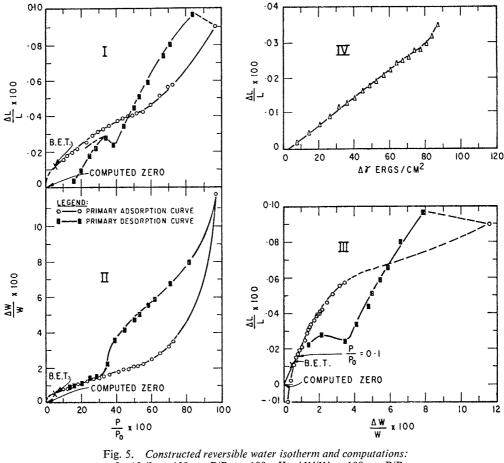


Fig. 5. Constructed reversible water isotherm and computations: $I = \Delta L/L \times 100 \text{ vs. } P/P_0 \times 100; II = \Delta W/W \times 100 \text{ vs. } P/P_0 \times 100; III = \Delta L/L \times 100 \text{ vs. } \Delta W/W \times 100; IV = \Delta L/L \text{ vs.} \Delta y.$

zero (14-17). Thus it is concluded that a larger amount of 'irreversible water' is removed below P/P_0 of 0.10, and so the physically held water cannot be estimated in this region using loops 1 or 2. An alternative procedure was used to achieve this. The N₂ surface area of $30 \text{ m}^2/\text{g}$ (Table 1) was assumed to be approximately correct. Then, using the B.E.T. equation and adding different amounts of reversible water to represent that adsorbed below a P/P_0 of 0.10, calculations were made allowing the assumed surface area to vary slightly, until the monolayer capacity fell on a P/P_0 of 0.15 to 0.20. Using the area of the water molecule as $10.8 \text{ m}^2/\text{g}$, the water area obtained was $40.8 \text{ m}^2/\text{g}$; 0.70 per cent for $\Delta W/W \times 100$ was used for the 'reversible water' between P/P_0 of 0 to 0.10. From the B. E. T., a $\Delta W/W$ value for P/P₀ of 0.05 was obtained, and all other points below this were made by extrapolation of the curve. No significance was attributed to values below P/P_0 of 0.05 for 'reversible water.' Similar values for $\Delta L/L$ could be obtained by extrapolation of the $\Delta L/L$ vs. $\Delta W/W$ plot to the zero obtained for $\Delta W/W$.

All these results are included in Table 3 together with the results for the 'irreversible water,' which will be discussed together in more detail later.

Application of Gibbs' Equation and the Estimation of Young's Modulus from the Reversible Isotherm

An integration over the adsorption branch of the reversible isotherm was made between P/P₀ values of 0.05 (to avoid the extrapolated area and errors in integration as the pressure approaches zero) and 0.60, according to Gibbs' equation (Eqs. (1) and (3)). The change in state of stress of the solid $\Delta\gamma$, is plotted against $\Delta L/L$ according to Eq. (4). As shown on Fig. 5, this plot yields a very good straight line, and it appears that the whole procedure in constructing the reversible isotherm is justified. The slope of this line, k_1 , from Eq. (4) is 3.90×10^{-6} cm/dyne.

| P/P ₀ range | Sorbed | | Reversibly desorbed | | | | Irreversibly Sorbed | | | | % lrr.* of Total sorbed | | % Rev.** of Total sorbed | | |
|-----------------------------|-------------------------|----------------------------|-----------------------|-------|-------------------------|-------|-------------------------|-----------|-------------------------|----------|----------------------------|--------------|-----------------------------|----------|--|
| | $\Delta W/W \times 100$ | $\Delta L/L \times 100$ | Δ W/W × 100 | Total | $\Delta L/L \times 100$ | Total | $\Delta W/W \times 100$ | Total | $\Delta L/L \times 100$ | Total | ∆W/W | $\Delta L/L$ | ΔW/W | ΔL/L | |
| 0 → 0.003 | 1.27 | 0.084 | _ | _ | _ | _ | _ | | - | - | - | _ | _ | · | |
| $0.003 \rightarrow 0.03$ | 1.25 | 0.098 | 0.71 | — | 0.063 | — | 0.54 | | 0.035 | | | — | _ | | |
| $0.03 \rightarrow 0.052$ | 0.56 | 0.040 | 0.20 | — | 0.012 | _ | 0.36 | | 0.028 | | — | — | — | | |
| $0.052 \rightarrow 0.08$ | 0.26 | 0.022 | 0.19 | — | 0.009 | | 0.07 | — | 0.013 | _ | | — | _ | — | |
| $0.08 \rightarrow 0.10$ | 0.18 | 0.013 | 0.11 | | 0.004 | | 0.07 | | 0.009 | | _ | — | _ | - | |
| $0 \rightarrow 0.10$ | 3.52 | 0.257 | 0.70 | 0.70 | 0.016 | 0.016 | 2.82 | 2.82 | 0.241 | 0.241 | 80.1 | 93.8 | 19.9 | 6.2 | |
| $0.10 \rightarrow 0.123$ | 0.16 | 0.011 | 0.10 | 0.80 | 0.002 | 0.018 | 0.06 | 2.88 | 0.009 | 0.250 | 78.3 | 93.3 | 21.7 | 6.7 | |
| $0.123 \rightarrow 0.15$ | 0.16 | 0.010 | 0.11 | 0.91 | 0.002 | 0.020 | 0.05 | 2.93 | 0.008 | 0.258 | 76.4 | 92.8 | 23.6 | 7.2 | |
| $0.15 \rightarrow 0.18$ | 0.15 | 0.009 | 0.11 | 1.02 | 0.002 | 0.022 | 0.04 | 2.97 | 0.007 | 0.265 | 74.4 | 92.3 | 25.6 | 7.7 | |
| $0.18 \rightarrow 0.234$ | 0.28 | 0.017 | 0.18 | 1.20 | 0.004 | 0.026 | 0.10 | 3.07 | 0.013 | 0.278 | 71.9 | 91.4 | 28.1 | 8.6 | |
| $0.234 \rightarrow 0.27$ | 0.22 | 0.009 | 0.10 | 1.30 | 0.004 | 0.030 | 0.12 | 3.19 | 0.005 | 0.283 | 71.0 | 90.4 | 29.0 | 9.6 | |
| $0.27 \rightarrow 0.30$ | 0.18 | 0.008 | 0.09 | 1.39 | 0.002 | 0.032 | 0.09 | 3.28 | 0.006 | 0.289 | 70.2 | 90.0 | 29.8 | 10.0 | |
| $0.30 \rightarrow 0.33$ | 0.20 | 0.009 | 0.08 | 1.47 | 0.001 | 0.033 | 0.12 | 3.40 | 0.008 | 0.297 | 69.5 | 90.0 | 30.5 | 10.0 | |
| $0.33 \rightarrow 0.36$ | 0.20 | 0.007 | 0.09 | 1.56 | 0.002 | 0.035 | 0.11 | 3.51 | 0.005 | 0.302 | 69.2 | 89.6 | 30.8 | 10.4 | |
| $0.36 \rightarrow 0.414$ | 0.30 | 0.013 | 0.16 | 1.72 | 0.002 | 0.037 | 0,14 | 3.65 | 0.011 | 0.313 | 68.0 | 89.4 | 32.0 | 10.6 | |
| $0.414 \rightarrow 0.44$ | 0.13 | 0.006 | 0.12 | 1.84 | 0.002 | 0.039 | 0.02 | 3.67 | 0.004 | 0.317 | 66.6 | 89.1 | 33.4 | 10.9 | |
| $0.44 \rightarrow 0.47$ | 0.15 | 0.010 | 0.05 | 1.89 | 0,001 | 0.040 | 0.10 | 3.77 | 0.009 | 0.326 | 66.6 | 89.1 | 33.4 | 10.9 | |
| $0.47 \rightarrow 0.50$ | 0.17 | 0.008 | 0.12 | 2.01 | 0.001 | 0.041 | 0.05 | 3.82 | 0.007 | 0.333 | 65.5 | 89.1 | 34.5 | 10.9 | |
| $0.50 \rightarrow 0.52$ | 0.14 | 0.005 | 0.05 | 2.06 | 0.001 | 0.042 | 0.09 | 3.91 | 0.004 | 0.337 | 65.5 | 88.9 | 34.5 | 11.1 | |
| $0.52 \rightarrow 0.55$ | 0.28 | 0.013 | 0.12 | 2.18 | 0.001 | 0.043 | 0.16 | 4.07 | 0.012 | 0.349 | 65.1 | 89.1 | 34.9 | 10.9 | |
| $0.55 \rightarrow 0.60$ | 0.52 | 0.014 | 0.26 | 2.44 | 0.004 | 0.047 | 0.26 | 4.33 | 0.010 | 0.359 | 64.0 | 88.4 | 36.0 | 11.6 | |
| $0.60 \rightarrow 0.65$ | 0.65 | 0.015 | 0.32 | 2.72 | 0.005 | 0.052 | 0.33 | 4.66 | 0.010 | 0.369 | 63.2 | 87.7 | 36.8 | 12.3 | |
| $0.65 \rightarrow 0.70$ | 0.82 | 0.017 | 0.41 | 3.13 | 0.005 | 0.057 | 0,41 | 5.07 | 0.012 | 0.381 | 61.8 | 87.0 | 38.2 | 13.0 | |
| $0.70 \rightarrow 0.727$ | 0.53 | 0.009 | 0.29 | 3.42 | 0.001 | 0.058 | 0.24 | . 5.31 | 0.008 | 0.389 | 60.8 | 87.0 | 39.2 | 13.0 | |
| 0.727 → 0.97 | 10.58 | 0.082 | 8.32 | 11.74 | 0.035 | 0.093 | 2.26 | 7.57 | 0.047 | 0.436 | 39.2 | 82.4 | 60.8 | 17.6 | |
| P/P ₀ range | Desc | Desorbed Reversibly sorbed | | | I | lr | reversib | ly desorb | ed | Comments | | | | | |
| 0.97 → 0.29 | 10.37 | 0.073 | 10.37 | 1.37 | 0.073 | 0.020 | _ | 7.57 | | 0.436 | Assum | ed no inte | erlayer wate | er lost | |
| $0.29 \rightarrow 0.25$ | 0.27 | 0.006 | 0.15 | 1.22 | 0.005 | 0.015 | 0.12 | 7.45 | 0.001 | 0.435 | | - | _ | | |
| $0.25 \rightarrow 0.20$ | 0.39 | 0.011 | 0.19 | 1.03 | 0.008 | 0.007 | 0.20 | 7.25 | 0.003 | 0.432 | | - | | | |
| $0.20 \rightarrow 0.16$ | 0.24 | 0.009 | 0.15 | 0.88 | 0.007 | 0.000 | 0.09 | 7.16 | 0.002 | 0.430 | | - | _ | | |
| $0.16 \rightarrow 0.14$ | 0.13 | 0.006 | 0.07 | 0.81 | 0.003 | — | 0.06 | 7.10 | 0.003 | 0.427 | | - | | | |
| $0.14 \rightarrow 0.05$ | 0.96 | 0.060 | 0.35 | 0.46 | 0.007 | | 0.61 | 6.49 | 0.053 | 0.374 | | ated from | | | |
| $0.05 \rightarrow 0.044$ | 0.20 | 0.017 | 0.03 | 0.43 | 0.001 | | 0.17 | 6.32 | 0.017 | 0.357 | Estima | ted value | s of reversil | ble wate | |
| $0.044 \rightarrow 0.036$ | 0,26 | 0.022 | 0.05 | 0.38 | 0.001 | — | 0.21 | ,6.11 | 0.021 | 0.336 | " | | | | |
| $0.036 \rightarrow 0.023$ | 0.44 | 0.035 | 0.07 | 0.31 | 0.002 | — | 0.37 | 5.74 | 0.033 | 0.303 | " | | | | |
| $0.023 \rightarrow 0.022$ | 0.43 | 0.028 | | | _ | _ | 0.43 | 5.31 | 0.028 | 0.275 | | " | | | |
| $0.022 \rightarrow 0.0093$ | 1.03 | 0.070 | 0.10 | 0.21 | | | 0.93 | 4.38 | 0.070 | 0.205 | | | " | | |
| $0.0093 \rightarrow 0.0042$ | 1.14 | 0.125 | 0.21 | 0.00 | _ | | 0.93 | 3.45 | 0.125 | 0.085 | | | " | | |
| $0.0042 \rightarrow 0$ | 3.38 | 0.485 | - | _ | _ | | 3.38 | 0.07 | 0.485 | -0.400 | Actual value is -0.4200 | | | | |

Table 3. Computed values for the reversible and irreversible isotherms

* Total irreversible sorbed **Total reversibly desorbed

Using a value of 2.86 g/cc for $Ca_3Si_2O_7 \cdot 2H_2O$ (18) since at a P/P_0 of 0.30 only about 40 per cent of the irreversible water has re-entered and since most of the adsorption is taking place on this "crystal" which constitutes most of the area, and using 40.8 m^2/g for the surface area, the value of 'E' from Eq. (5) is 2.99 \times 10¹¹ dyne/cm² or 4.35 \times 10⁶ lb/in.². This value is about 8 times as large as that measured for the equivalent compact (19), or of the equivalent water to cement ratio paste (20). This calculated value, however, represents 'E' for the solid material, not the porous body. Helmuth and Turk (20) extrapolated from porosity-E plots to get 'E' of 'gel phase' as 4.5, and of 'solid phase' 10.8 (lb/in.2). This latter value was similar to the extrapolation of Soroka and Sereda (19). Both these values suffer from the difficulty of measuring the correct porosity; however, since a large part of the water removed during 'd-drying' is interlayer water which returns on sorption. Thus, the water

porosity (determined by water) would be much lower than anticipated, making the extrapolated value much too high. Considering these assumptions, the value found for the modulus of the solid phases is very good and is considered as further evidence of the validity of this approach.

The Irreversible Isotherm

The method outlined in the previous section (construction of a reversible isotherm) also enables one to obtain the irreversible isotherm (Fig. 6 and Table 3). The large hysteresis in both length and weight change isotherms is evident. As already described, this hysteresis exists even to vapour pressures of only a few microns. The 'irreversible water' is sorbed at all pressures along the primary adsorption isotherm, and this explains why the time to attain equilibrium was always longer on this curve. Values below P/P_0

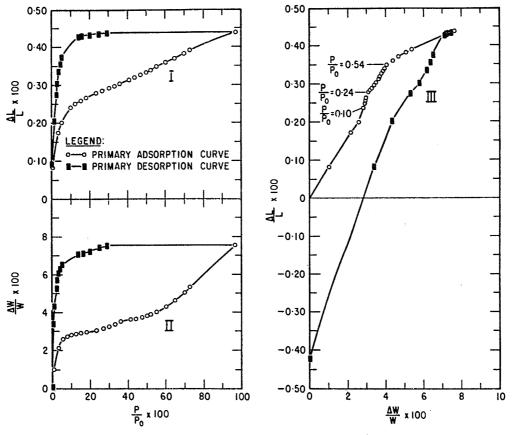


Fig. 6. Constructed irreversible water isotherm: $I = \Delta L/L \times 100$ vs. P/P₀ × 100; $II = \Delta W/W \times 100$ vs. P/P₀ × 100; $III = \Delta L/L \times 100$ vs. $\Delta W/W \times 100$.

of 0.05 were extrapolated for 'reversible water', but since this became small compared with the 'irreversible water', any error would be negligible.

The plot of the $\Delta L/L$ vs. $\Delta W/W$ shows the important change in slope on the sorption curve at P/P₀ of 0.54. This is precisely the point where the value of the modulus of elasticity (11) starts to increase, when measured as a function of relative pressure. In addition, the hysteresis of this curve shows that the withdrawal of interlayer water follows a completely different path from its entry. Again this might be implied from the results of the modulus measurements (11). As the desorption continued, it appeared as if the loop might gradually close, but below P/P₀ of 0.009 it diverged yielding a large irreversible shrinkage below the original zero by 0.420 per cent, although the zero for $\Delta W/W$ was the same.

This irreversible effect also occurred on the first degassing, but did not occur when degassing took place after a methanol cycle. Thus it must be associated with the effect of water. Solution effects of water on calcium hydroxide (14) are ruled out because the effect is considered too large; the explanation favoured is that when the final interlayer water is expelled, a reorientation of the layers occurs, resulting in an irreversible contraction. More work is needed in this area. Nevertheless, a plausible model can be suggested to explain most of the general behaviour of the entrance and exit of interlayer water and the variation of $\Delta L/L$ and modulus of elasticity with P/P₀.

Fig. 7 illustrates in model form the process of exit and entry of interlayer water: initially drying will take place from the edges with little contraction ((a) to (b)); drying to state (c) will provide some collapse and large contraction; drying at the edges probably occurs below P/P_0 of 0.30 and stronger drying (state (c)), below P/P_0 of 0.07; the final removal of the water in the middle will not take place above P/P_0 of 0.009. It is considered that this water in the centre provides the main bracing for a higher rigidity and, when it is removed, the modulus decreases as experiments show. This state of drying (d) also involves possible reorientation of the plates to produce an irreversible contraction. Resorption now occurs

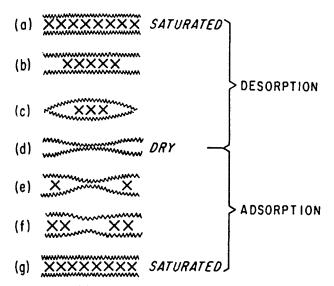


Fig. 7. Simplified model for exit and entry of water between layers of tobermorite gel

at the edges (states (e) and (f)), being initiated by physical adsorption and resultant surface free energy change on the external surfaces. Here, the pressure vs. $\Delta L/L$ or $\Delta W/W$ hysteresis is apparent, since interlayer water cannot enter until some external movement occurs. Further sorption will continue inward from the edges, causing large expansions. As the layers are filled towards the middle (states (f) to (g)), it is apparent that the modulus will start to increase due to "bracing" of the layers by the water molecules; the resultant $\Delta L/L$ will not be as large because most of the expansion occurred from the edges.

Further implications of the interlayer water can be observed from Table 3:

(a) Total interlayer water for this sample is 7.54 per cent, although it may be somewhat higher, as discussed above. This means that the difference between pore volumes obtained by water, on the one hand, and nitrogen and methanol, on the other, would be in the order of 0.08 ml/g. This explains the discrepancies in pore volume obtained by Mikhail and Selim (21) for pastes with a w/c of 0.35 to 0.57. It is postulated here that, since the interlayer penetration by nitrogen is very small, this gas would give the best pore volume for mechanical property extrapolations.

(b) Less than 20 per cent of the total expansion along the isotherm is due to physically adsorbed water. The percentages of physical and 'irreversible' water, and their concomitant length changes for the different pressure ranges are shown in Table 3.

The only remaining evidence to support the pre-

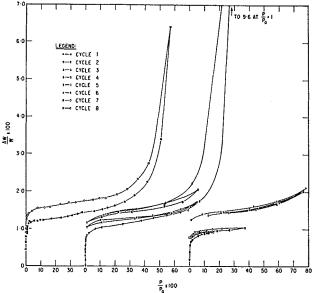


Fig. 9. Length change isotherms of methanol on bottle-hydrated portland cement compacts degassed at 80°C.

vious model of hydrated portland cement is the density measurements of Brunauer, Kantro, and Copeland (18). It is clear, however, that when the density is measured with a water solution, the interlayer water has already re-entered. The slow decrease in density obtained by these authors for some less severely dried samples is probably associated with some slow recovery of the irreversible shrinkage observed by Helmuth and Turk (22), or as observed here below P/P_0 of 0.009. Density measurements should be perhaps obtained with nitrogen.

Methanol Adsorption

Methanol sorption was measured on the same compacted sample degassed at 80°C.

The sorption results (Fig. 8) are very similar to those obtained by Mikhail (21) inasmuch as a surface area of similar magnitude was obtained (area of molecule taken as 18.1 Å^2 , see Table 1), and the low pressure hysteresis is of the same magnitude (intermediate between water and nitrogen). Several cycles were performed, however, and length change measurements, (Fig. 9) were made during these cycles. Significant features of these results are the following:

(a) After significant sorption at very low pressures, the isotherm is very flat; for cycle 2 to P/P_0 of 0.75 the desorption is even flatter. This may be explained by the concept of autophobicity of alcohol adsorption (23), where the isotherms exhibit strong monolayer

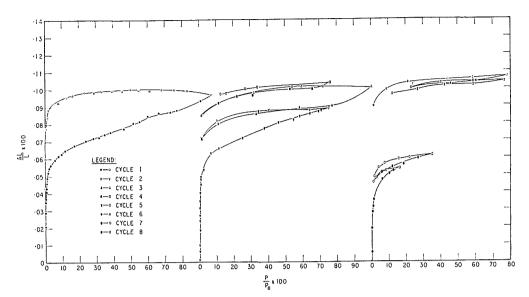


Fig. 8. Sorption isotherms of methanol on bottle-hydrated portland cement compacts degassed at 80°C.

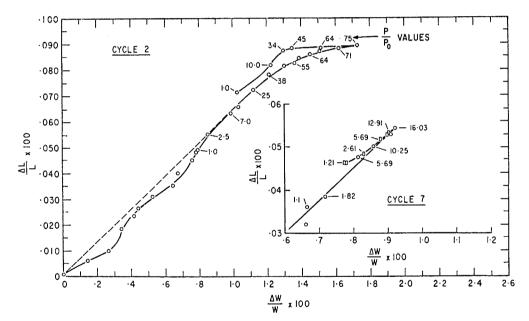


Fig. 10. $\Delta L/L$ vs. $\Delta W/W$ plots for methanol sorbed on bottlehydrated portland cement compact degassed at $80^{\circ}C$ (P/P₀ values are \times 100)

binding with little tendency toward multilayer formation; multilayer formation occurred almost asymptotically at high vapour pressures. The autophobicity is due to strongly oriented adsorption in the first adsorbate layer which would permit multilayer formation at a distance remote from the initial interface so that its influence is lost. The result would approximate to a Langmuir isotherm, but for methanol, whose hydrocarbon chain is not so long, this approximation is not completely attained.

(b) Cycles 2, 7 and 8 show that the hysteresis, like that for water, is cumulative, significant low pressure hysteresis occurring even after sorption to only P/P_0 of 0.17. Cycle 3 rejoins precisely where cycle 2 stopped on the adsorption curve, but for cycles 7 and 8, the rejoining is not so exact. Cycle 4 shows that some of the irreversibly sorbed methanol may be withdrawn at about P/P_0 of 0.01; cycle 5 shows that the isotherm

is close to reversible between P/P_0 of 0.12 and 0.77 on the descending branch, and cycle 6, that some irreversible sorbed methanol is added when this cycle goes to a higher pressure than did cycles 4 and 5.

(c) The length results show the same result as far as irreversibility is concerned. The ascending 'sorption' curves, however, cycles 1, 2, 3, show a significant length change at the beginning and all the way up the isotherm, contrary to the assumption of Mikhail and Selim (21). Despite the large desorption, there is very little contraction on the desorption curve. This length change plot looks very similar to the constructed irreversible plot for water. The explanation is clear: along the sorption curve, both physical adsorption (of a strong nature at low P/P_0), and interlayer penetration are taking place. The penetration is less than that of water because of the respective sizes of the molecules; on the desorption curve only weakly held methanol is coming off. At P/P_0 of 0.10, the slope $(\Delta L/L)/(\Delta W/W)$ for the hysteresis is taken to represent that for interlayer methanol (see Table 1); the value 0.0955 is more than that for water (0.0860) which is reasonable since the methanol molecule is bigger than water. Curve I in Fig. 10 shows the $\Delta L/L$ vs. $\Delta W/W$ plot. The points below P/P₀ of 0.01 show signs of specific interaction, but the adsorbed methanol cannot be separated from the interlayer methanol. If the average slope is taken and the surface area is assumed to be $30 \text{ m}^2/\text{g}$ (nitrogen value), the physically adsorbed methanol will have a $(\Delta L/L)/(\Delta W/W)$ of 0.0525, over twice that for water. This is consistent with Gibbs' equation if, as assumed, a larger proportion of the methanol is adsorbed at low pressures. There would be reason to expect that the specific adsorption for methanol would be different from the one for water if the surface contains many hydroxyl groups (13). Details of this will not be included here, but it is apparent that the methanol isotherm is more complicated than previous interpretations (21), and that it is consistent in every way with the results obtained from water sorption.

Conclusions

1. Exposure of dried (below approximately 10 per cent R. H.) hydrated portland cement paste to water vapour at any pressure results in the entry of interlayer hydrate water simultaneously with physically adsorbed water.

2. Surface areas are much lower than was believed, the nitrogen area probably being the most reliable figure.

3. Less than 18 per cent of the expansion along the isotherm is due to physically adsorbed water.

4. Porosity values obtained from water sorption are too high. Nitrogen would give more reliable figures.

5. Gibbs' equation is obeyed for the constructed reversible isotherm, and a calculation of the modulus of elasticity of the solid material gives a reasonable value.

6. A model for the entry and exit of interlayer water is given which explains the effect of vapour pressure on the modulus of elasticity. This model suggests that the entry and exit of interlayer hydrate water plays an important part in creep phenomena.

7. Results from methanol sorption, which also involves interlayer penetration, are consistent with those of water.

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