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### **Multivariate factor analysis of heavy minerals concentrate from Athabasca Oil Sands tailings by XPS**

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# MULTIVARIATE FACTOR ANALYSIS OF HEAVY MINERALS CONCENTRATE FROM ATHABASCA OIL SANDS TAILINGS BY XPS

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Canada

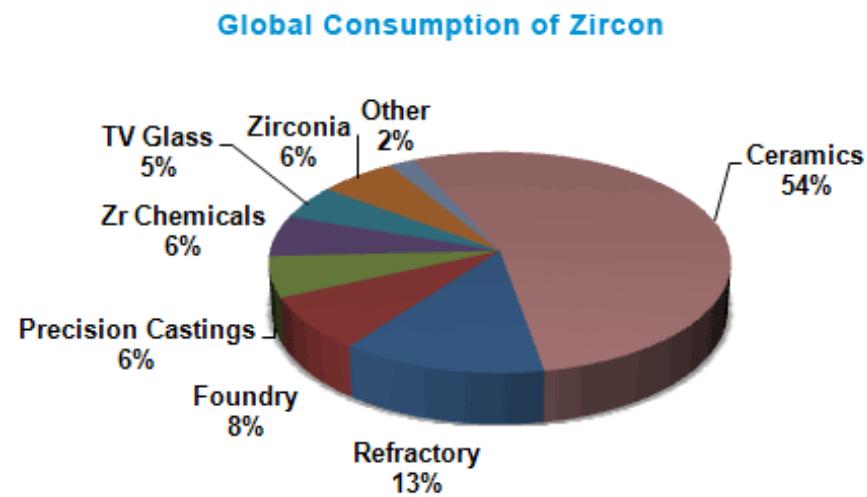
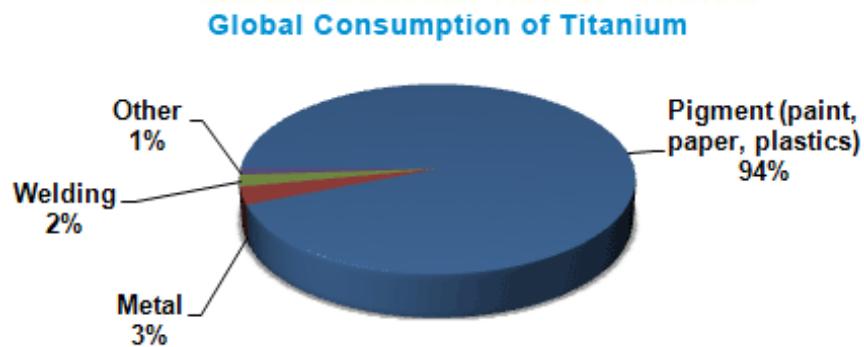
# Presentation Overview :

- 1) Motivation & Research Objectives
- 2) Multivariate Factor Analysis
- 3) Large-Area Spectroscopy
- 4) Surface Component Imaging

# Motivation & Research Objectives

## Commercial Oil Sands Processing

- hot water extraction → bitumen froth floatation / tailings solids
- heavy mineral solids concentrate in froth



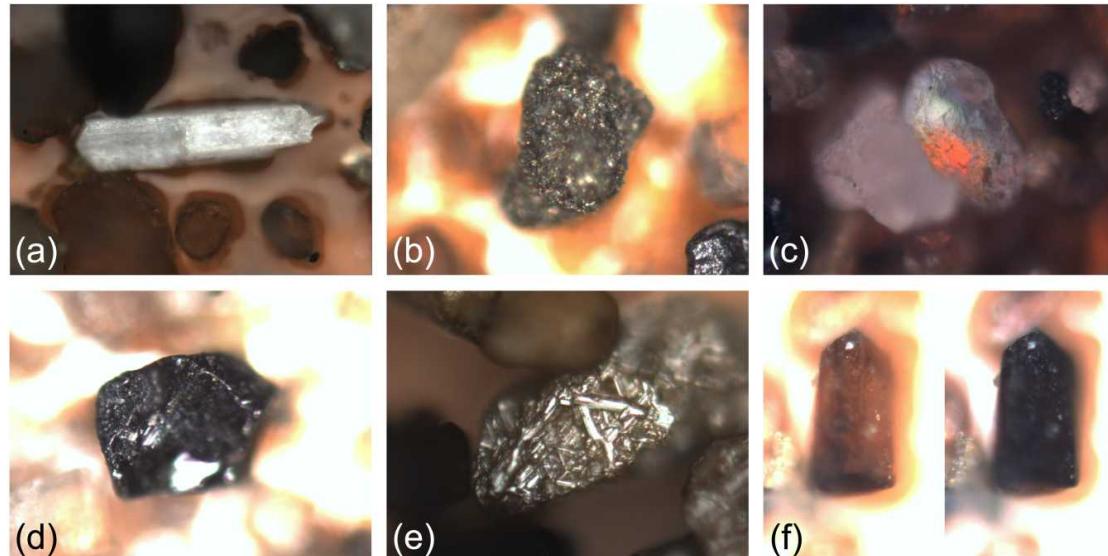
<http://www.titaniumcorporation.com>



# Motivation & Research Objectives

Electrostatic and magnetic separation of HMC

- f) zircon ( $ZrSiO_4$ ); e) rutile ( $TiO_2$ ); d) ilmenite ( $FeTiO_3$ )
- c) quartz ( $SiO_2$ ); b) pyrite ( $FeS_2$ ); a) gypsum ( $CaSO_4 \cdot 2H_2O$ )



100-200  $\mu m$

XPS study ←  
1) mineral associations  
2) surface condition

# Multivariate Factor Analysis

Principal Components Analysis (PCA)  $X = SV^T$

- variable reduction
- scores (S) & loadings (V)
- orthogonal factors (uncorrelated)
- within factor variable correlations

## Spectral Analysis

$$\begin{matrix} m \times n \\ X \end{matrix} = \begin{matrix} m \times n_p \\ U \end{matrix} \begin{matrix} n_p \times n_p \\ \Sigma \end{matrix} \begin{matrix} n_p \times n \\ V^T \end{matrix}$$

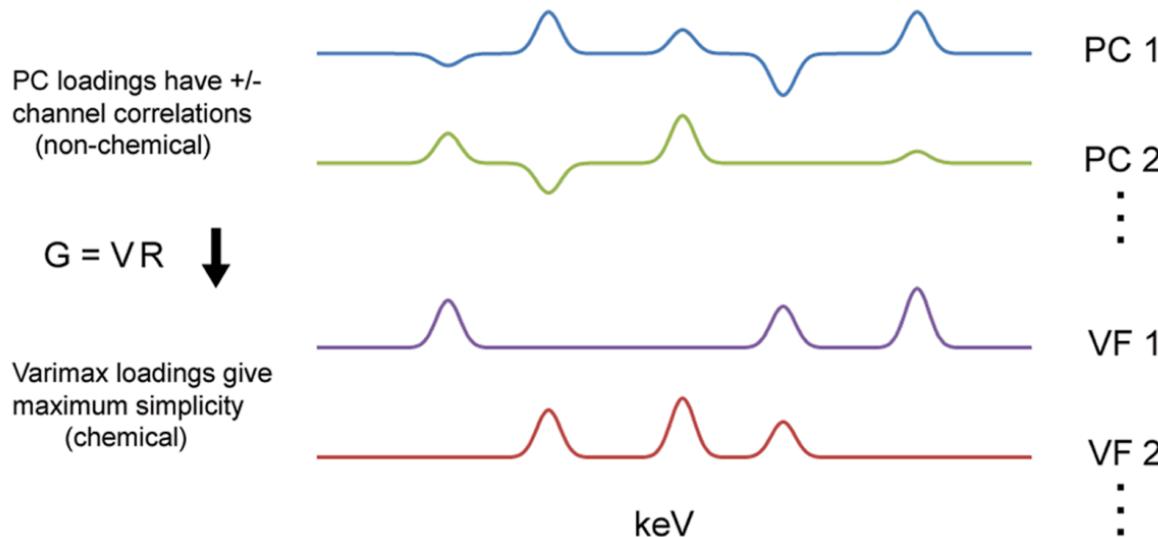
The diagram illustrates the Singular Value Decomposition (SVD) of a matrix X. Matrix X is of size m x n. It is equal to the product of three matrices: U (m x n<sub>p</sub>), Σ (n<sub>p</sub> x n<sub>p</sub> diagonal matrix with entries like \*, \*, \*, \*, \*, \*), and V<sup>T</sup> (n<sub>p</sub> x n).

- PCA factorization by SVD
- component & spectral bases
- ordered by significance
- noise reduction

# Multivariate Factor Analysis

Varimax rotation (R)

- improves factor interpretability
- component or spectral maximum simplicity\*



\* few minerals / spot, or  
few elements / spectrum

Varimax criterion

$$\max \sum_j \sigma_j^2 (V_{i,j}^2)$$

spectral basis

$$G = VR$$

or

component basis

$$H = UR$$

# Multivariate Factor Analysis

Varimax con't

- preserves orthonormality of rotated basis
- relaxed orthogonality in complementary domain

spectral basis

$$(VR)^T VR = I$$

component basis

$$(UR)^T UR = I$$

$$(U\Sigma R)^T U\Sigma R \neq D$$

$$(V\Sigma R)^T V\Sigma R \neq D$$

like factor  
modeling



- \* trade simplicity in one domain for contrast in other
- \* choose constraints based on physical characteristics

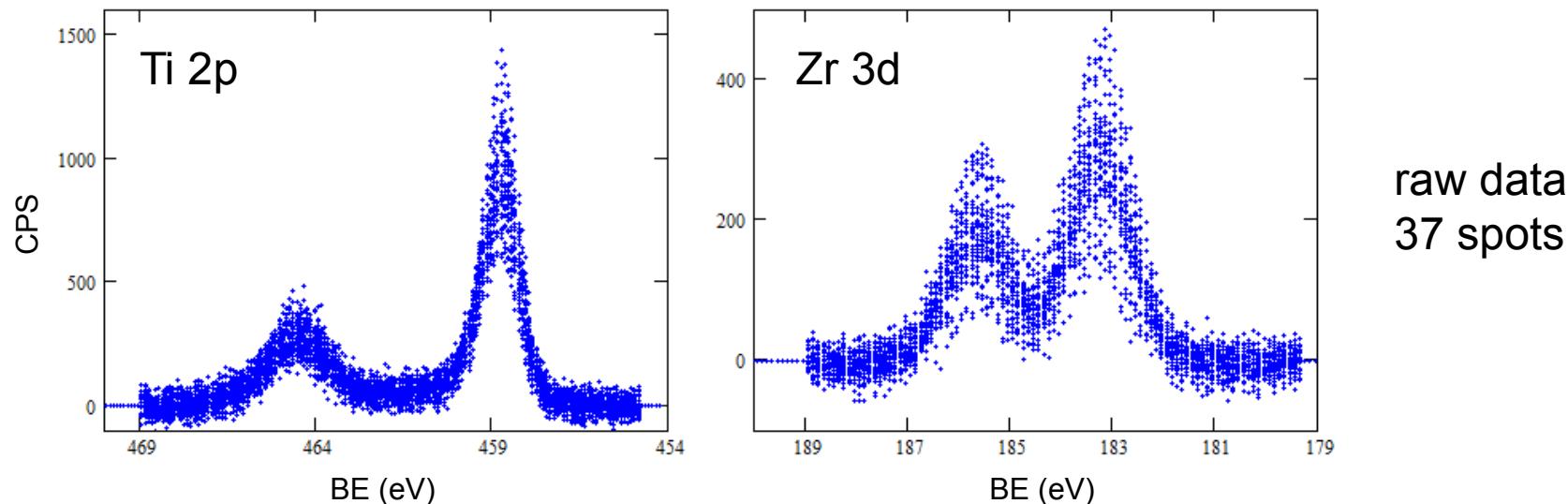
Keenan, M. R. *Surf. Interface Anal.* **2009**, 41, 79.

Smentkowski, V. S.; Ostrowski, S. G.; Keenan, M. R. *Surf. Interface Anal.* **2009**, 41, 88.

# Large-Area Spectroscopy

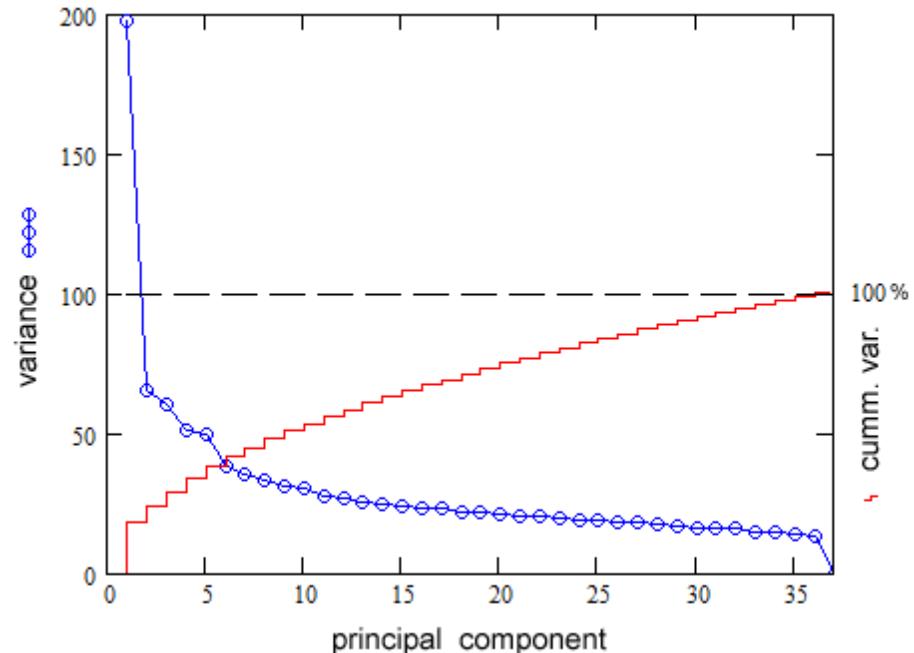
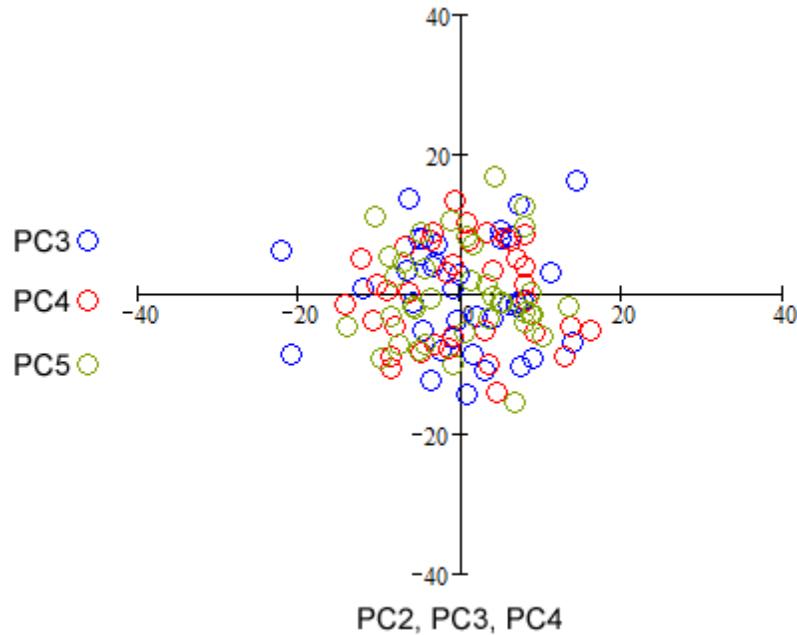
Measurement - 300 x 700  $\mu\text{m}$  spot area (5-10 particles per spot)

Pre-processing i) background subtraction / concatenate regions  
ii) standardization (mean-center / unit variance)



# Large-Area Spectroscopy

PCA score plot and variance (eigenvalues)



- no component classification
- 6 factors retained for spectral rotation

# Large-Area Spectroscopy

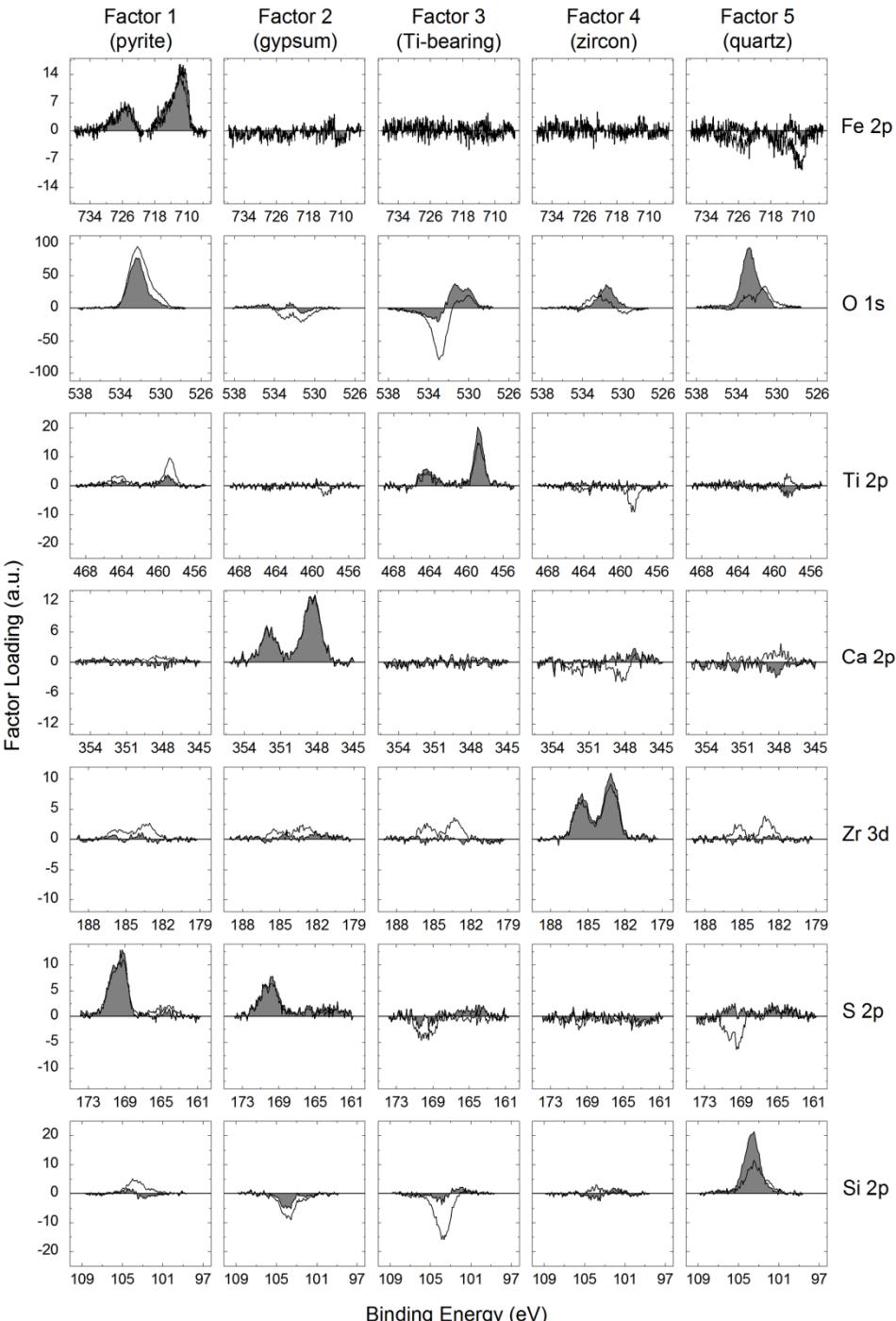
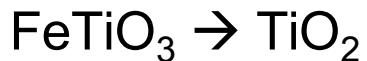
## Loadings Spectra ( $\sigma V$ and $\sigma VR$ )

- orthonormal  $V$  and  $VR$
- Varimax rotation (filled)
- PCA (solid line)

## Interpretation

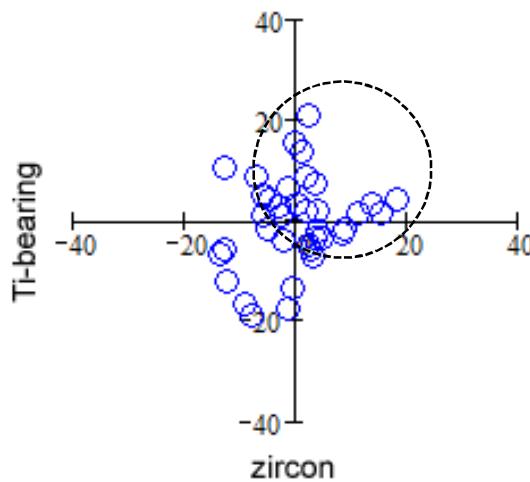
- simplifies factor correlations  
→ better chemical representation
- Ti-bearing: can't distinguish  $TiO_2$  from *altered ilmenite*

↓  
*weathering*  
spectral overlap

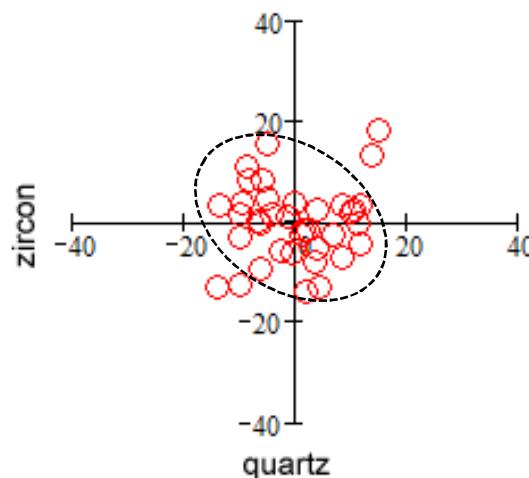


# Large-Area Spectroscopy

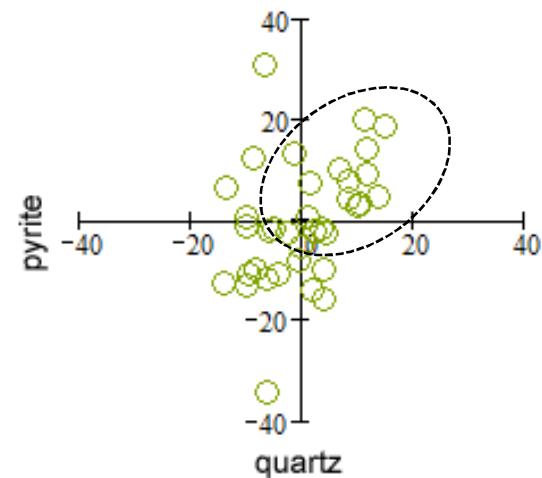
## Rotated Factor Scores



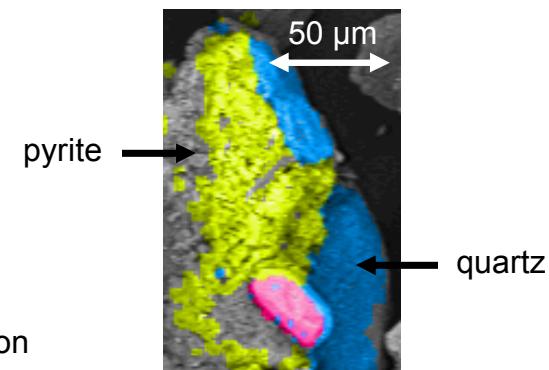
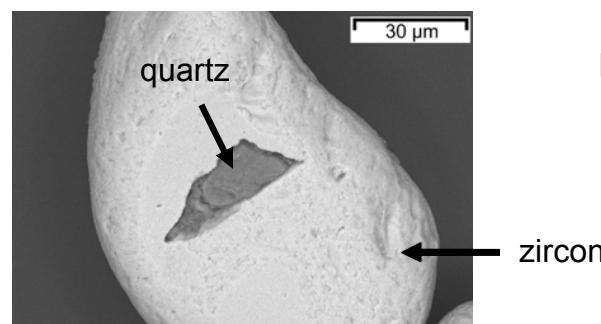
- large liberated particles
- electrostatic separation !



- some inclusion in smaller particles



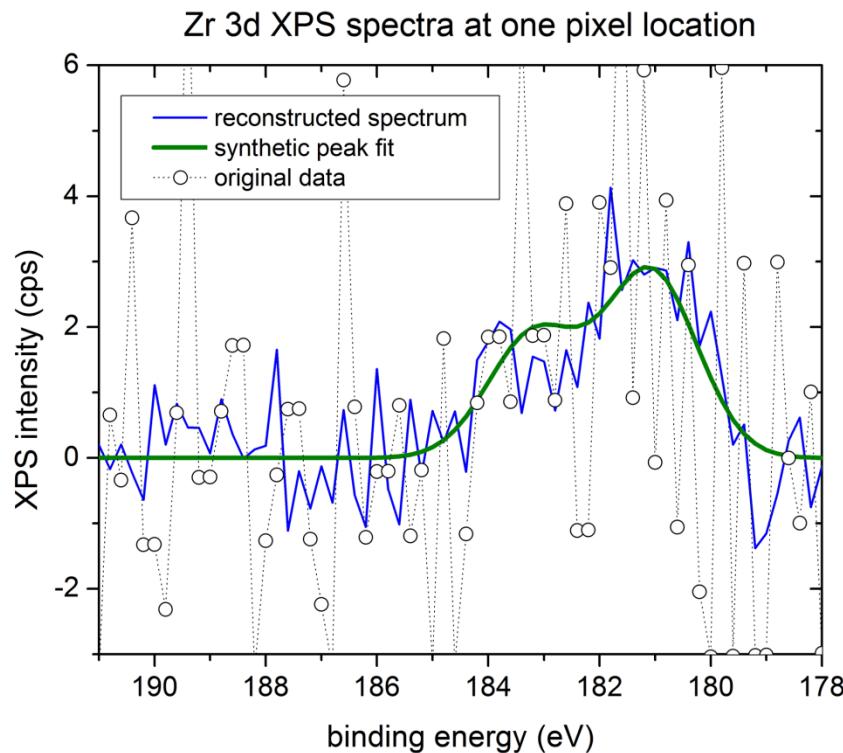
- physical association
- pyrite floatation



# Surface Component Imaging

## Data Cube

- 256 x 256 pixels ( $3 \times 3 \mu\text{m} / \text{pixel}$ )  $\sim 20 \mu\text{m}$  features
- 567 BE channels in 0.2 eV steps



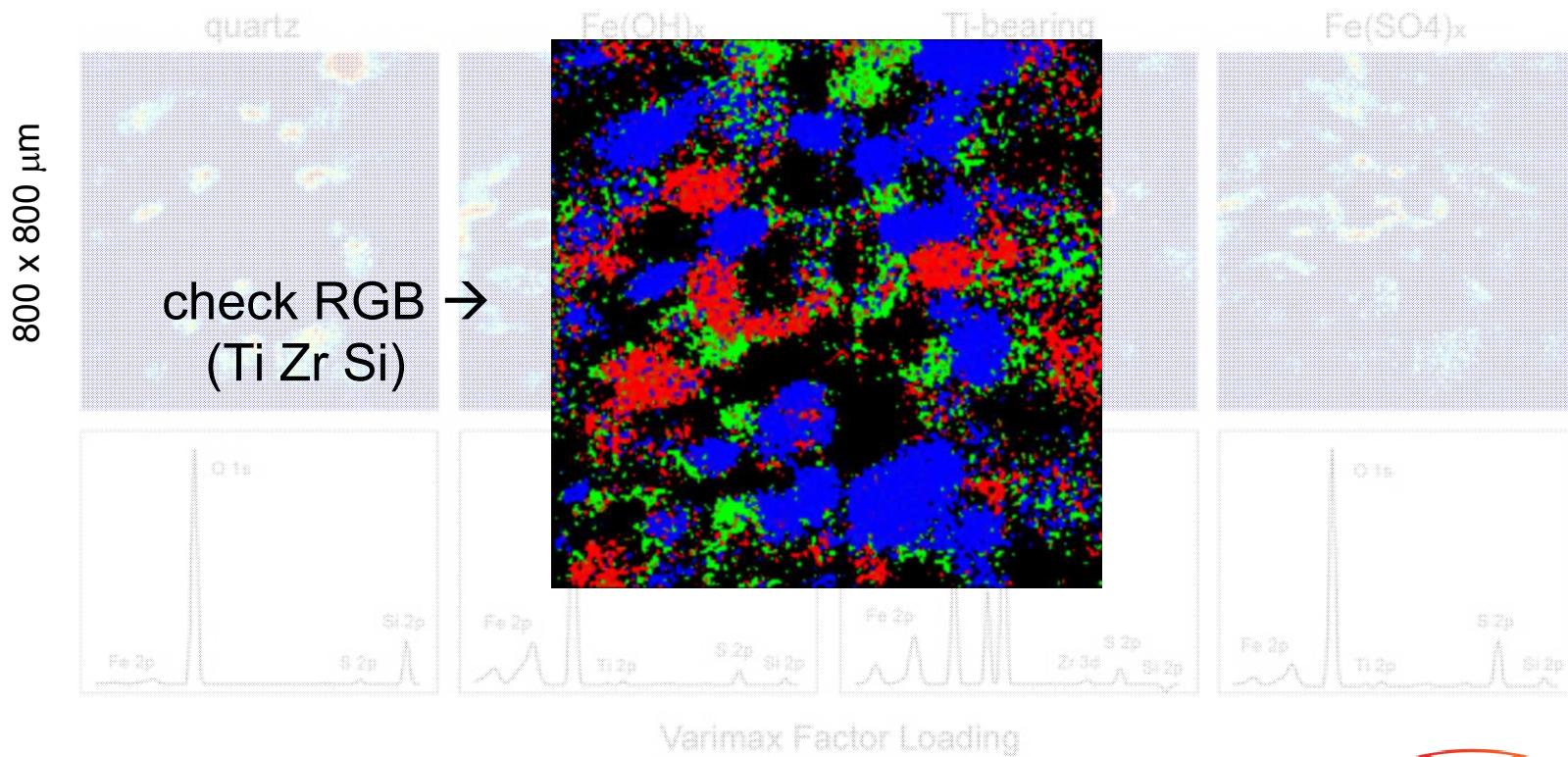
## PCA data reconstruction

- noise reduction / peak fitting
- spectral integration
- elemental RGB images

# Surface Component Imaging

Varimax Rotation (VΣR) on synthetic fit spectra

- orthonormal score images (UR), but w/o spatial simplicity
- surface components → pyrite weathering



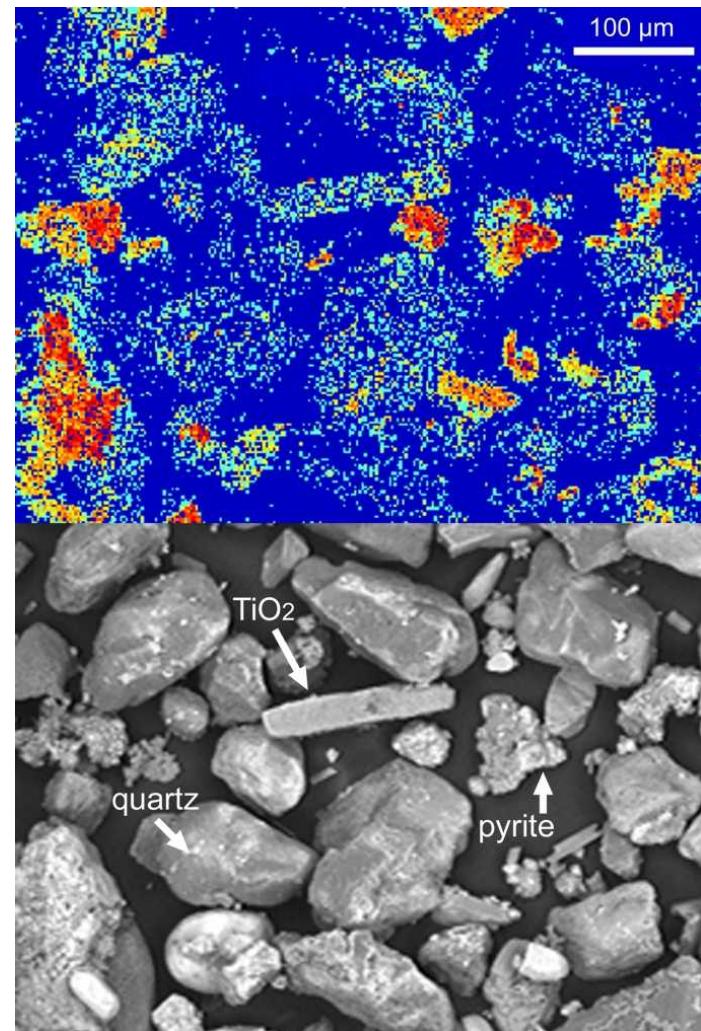
# Surface Component Imaging

check SEM-EDX

- sulphur channel  $K\alpha$  2.3 keV
- off-peak background subtraction
- compare to backscattering image



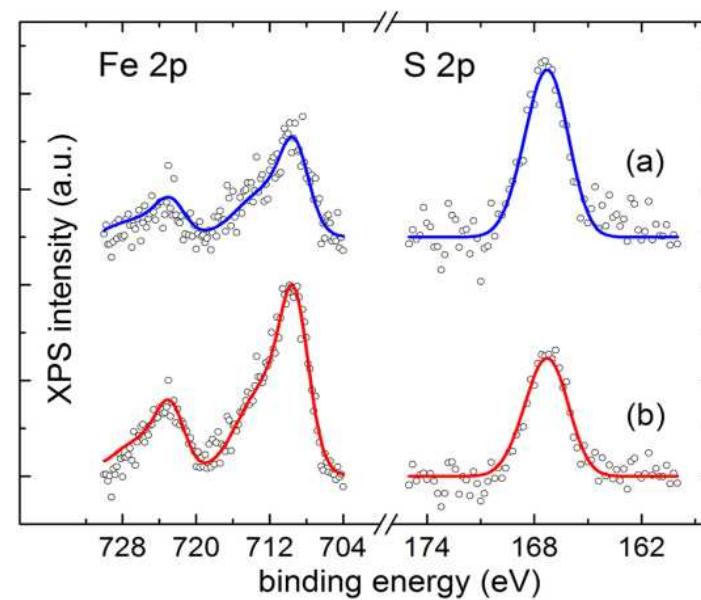
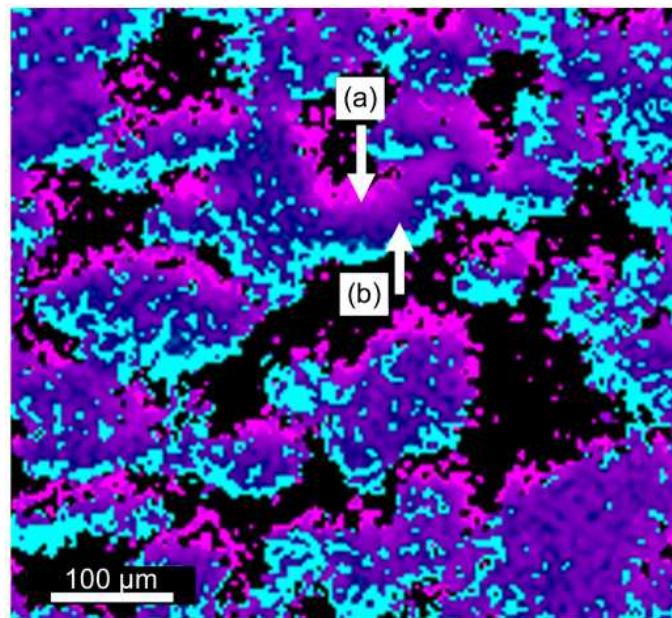
solid pyrite and surficial component



# Surface Component Imaging

check PCA reconstructed image

- Fe (cyan) and S (magenta)
- relative proportion maps to new vector in 3-colour space
- shadow effect suggests bi-layering



## Summary:

- LAS Varimax rotation VR → factor loadings like mineral chemistry
- LAS factor scores indicate mineral associations
  - i) particle liberation for Ti and Zr heavy minerals
  - ii) quartz / zircon inclusions
  - iii) pyrite / quartz physical association
- imaging Varimax rotation (VΣR) → uncorrelated score images (UR)
- surface components resolved consistent with pyrite weathering (iron hydroxides / iron sulphates)





## Acknowledgements:

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Council Canada

Conseil national  
de recherches Canada

