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# Publisher's version / Version de l'éditeur:

https://doi.org/10.1016/j.ijhydene.2009.08.083

International Journal of Hydrogen Energy, 35, 10, pp. 5001-5009, 2009

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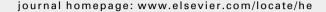


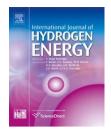




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# Effect of gasification agent on the performance of solid oxide fuel cell and biomass gasification systems

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#### ARTICLE INFO

Article history:
Received 18 June 2009
Received in revised form
11 August 2009
Accepted 30 August 2009
Available online 3 October 2009

Keywords:
Solid oxide fuel cell
Biomass
Gasification
Energy
Exergy
Efficiency

#### ABSTRACT

In this paper, an integrated solid oxide fuel cell (SOFC) and biomass gasification system is modeled to study the effect of gasification agent (air, enriched oxygen and steam) on its performance. In the present modeling, a heat transfer model for SOFC and thermodynamic models for the rest of the components are used. In addition, exergy balances are written for the system components. The results show that using steam as the gasification agent yields the highest electrical efficiency (41.8%), power-to-heat ratio (4.649), and exergetic efficiency (39.1%), but the lowest fuel utilization efficiency (50.8%). In addition, the exergy destruction is found to be the highest at the gasifier for the air and enriched oxygen gasification cases and the heat exchanger that supplies heat to the air entering the SOFC for the steam gasification case.

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# 1. Introduction

Biomass has increased its importance due to the fact that it can be utilized as a potential fuel source in advanced energy systems. In addition, systems based on biomass fuel are considered to contribute to the sustainable development in industrialized and developing countries. In this regard, researchers tend to find solutions to obtain efficient and economical heat and electricity generation from biomass fuel.

There are various types of biomass, such as wood, landfill gas, crops, alcohol fuels, and municipal solid wastes. Biomass has a share of 10.7% in the total global primary energy use and

1.1% in the world electricity production [1]. It is expected that the biomass share of electricity output will increase to a point between 2% and 5.1% in 2050 according to the different scenarios [2]. Conventionally, biomass is converted to electricity by combustion of the feedstock to generate steam that is used to drive the steam turbine. Other technologies include externally fired gas turbines, integrated gasification combined cycles, and fuel cells.

Among the different types of fuel cells, molten carbonate fuel cell (MCFC) and SOFC are considered as the most promising ones for biomass fuelled fuel cells due to their high operating temperature level, flexibility to different fuel, and

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greater tolerance to contaminants. According to the biomass conversion method, some of the other fuel cell types may also be useful. For example, landfill gas and digester gas may be used with phosphoric acid fuel cell (PAFC) today and their usage with this kind of fuel cell has been successfully demonstrated [3]. In addition, the suitability of biogas as a fuel for proton exchange membrane fuel cell (PEMFC) has been experimentally confirmed [4].

Biomass fuelled integrated SOFC system is one of the key energy technologies of the future since it combines the merits of renewable energy sources and hydrogen energy systems. There has been an increasing interest in converting biomass to a product gas by various thermochemical and biochemical methods for using it as a fuel in SOFCs. These methods include gasification, anaerobic digestion, fast pyrolysis, and fermentation. The product gas obtained from these conversions contains contaminants such as tars, hydrogen sulfide, and alkali compounds, which should be cleaned up according to the tolerance level of the SOFC to these contaminants. The cleaned gas exiting the gas cleanup system should be reformed to hydrogen and carbon monoxide to be utilized in the SOFC, which might be inside or outside the stack.

Panopoulos et al. [5,6] investigated the integration of a SOFC with a novel allothermal biomass steam gasification process. They calculated the electrical efficiency of the system as 36% and exergetic efficiency as 32%. Cordiner et al. [7] studied the integration of a downdraft gasifier with a SOFC in which woody material is used as the fuel. Electrical efficiency of the system was calculated as 45.8%. In the paper by Athanasiou et al. [8], integrated SOFC, steam turbine, and gasifier system was studied in terms of thermodynamics. The electrical efficiency of the system was found to be 43.3%. The comparison of cold gas cleanup and hot gas cleanup systems to be used in biomass gasification and SOFC system was done by Omosun et al. [9]. After taking into account thermodynamic and economical considerations, they concluded that hot gas cleanup should be preferred.

The main objective of this study is to develop a thermal model for an integrated SOFC and biomass gasification system

and investigate the effect of gasification agent on the performance of this system. For this purpose, thermodynamic models are developed for the system components, except SOFC, e.g. gasifier, afterburner, and blower. For the SOFC, a heat transfer model (see details in [10]) is employed. Some performance assessment parameters, namely: electrical efficiency, fuel utilization efficiency, power-to-heat ratio, and exergetic efficiency are studied. Also, exergy balances are written for the system components to calculate the exergy destructions within the system and exergy losses to the environment.

# 2. Description of the system

A schematic of the integrated biomass gasification and SOFC system is shown in Fig. 1. In this system, biomass enters the dryer to bring its moisture content to a level acceptable by the gasifier. According to the gasification agent, one of the following substances enters the gasifier: air, enriched oxygen or steam. The gas produced by gasification, which is called syngas, has high amounts of tar, sulphur and other contaminants which may cause degradation in SOFCs. Due to this fact, a gas cleanup should be used to clean the syngas according to the SOFC impurity levels. In this study, a hot gas cleanup is chosen. The cleaned syngas enters the SOFC, where electricity is produced. To prevent the carbon deposition, anode recirculation ratio is adjusted. The depleted fuel and air streams enter the afterburner to burn the unused fuel and increase the temperature of these streams. The burned gas mixture enters the heat exchanger to supply heat to the air entering the SOFC. The gas mixture leaving the heat exchanger supplies heat to the following devices: the steam generator and the gasifier in the case of steam gasification and the dryer. It is then emitted to the atmosphere.

A number is given to each state. In Fig. 1, states 20 and 22 are valid for both the air and enriched oxygen gasification cases. State 21 is only valid for enriched oxygen gasification case. State 13a, 13b, and 19 are only valid for the steam

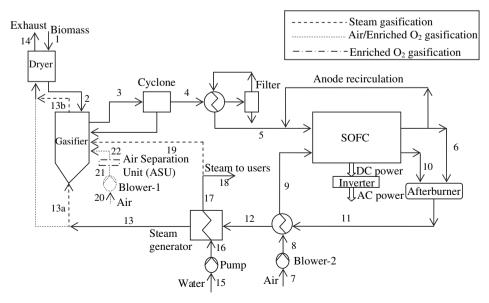


Fig. 1 - Schematic of the integrated biomass gasification and SOFC system.

gasification case. The differences in the configurations are represented with different dashed lines, which are labelled on Fig. 1.

# 3. Modeling

The main approach in the modeling is as follows. The syngas composition is first calculated using the gasifier model. Then, this composition and other SOFC operating parameters are used as input parameters in the heat transfer model of the SOFC. This model gives us the molar flow rate at the inlet and exit of gas channels, power output, and temperature at the exit of gas channels for a single cell. According to the power requirement of the SOFC, the number of SOFC stacks that must be used in this system is found. Then, using the output data from the gasifier and SOFC models, the molar flow rate of dry biomass is calculated. Using this molar flow rate and applying energy balances to the remaining components, the enthalpy flow rate of all states, work input to the blowers and pump, if applicable, are calculated.

The main assumptions in this model are as follows:

- The system operates at steady state.
- Kinetic and potential energy effects are ignored.
- Ideal gas principles apply for the gases.
- The syngas produced by the gasifier is at chemical equilibrium.
- The impurities such as tar, sulphur, ammonia are not considered in the calculations.
- Heat losses from the components are neglected.
- Work input for the high temperature blower for anode recirculation is neglected.
- All of the steam export returns as condensate.
- Complete combustion occurs in the combustor.

As an example, the modeling equations for the steam gasification case are given below.

The chemical reaction in the dryer may be shown as:

$$C_x H_v O_z + m_1 H_2 O_{(1)} \rightarrow C_x H_v O_z + m_2 H_2 O_{(1)} + (m_1 - m_2) H_2 O_{(v)}$$
 (1)

The gasification reaction may be given as:

$$\begin{split} C_{x}H_{y}O_{z}+m_{2}H_{2}O_{(l)}+(m_{1}-m_{2})H_{2}O_{(v)}+\lambda H_{2}O_{(v)}\\ +q_{added} \rightarrow \alpha_{1}CH_{4}+\alpha_{2}H_{2}+\alpha_{3}CO+\alpha_{4}CO_{2}+\alpha_{5}H_{2}O \end{split} \tag{2}$$

In Eq. (2), if we fix  $\lambda$ , there are six unknowns:  $\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5$ , and  $q_{\rm added}$ . We need six equations to find these unknowns. These equations are 3 atom balances, Eqs. (3)–(5), chemical equilibrium relations for water–gas shift reaction and methanation reaction, Eqs. (6) and (7), and the energy balance around the control volume enclosing the gasifier, Eq. (8).

$$\mathbf{x} = \alpha_1 + \alpha_3 + \alpha_4 \tag{3}$$

$$y + 2m_1 + 2\lambda = 4\alpha_1 + 2\alpha_2 + 2\alpha_5 \tag{4}$$

$$z + m_1 + \lambda = \alpha_3 + 2\alpha_4 + \alpha_5 \tag{5}$$

$$K_{\text{wgs}} = \exp\left[-\Delta \overline{g}_{\text{wgs}}^{\circ}/RT\right] = \frac{X_{\text{CO}_2} \cdot X_{\text{H}_2}}{X_{\text{CO}} \cdot X_{\text{H}_{2O}}}$$
(6)

$$K_{\rm m} = \exp\left[-\Delta \overline{g}_{\rm wgs}^{\circ}/RT\right] = \frac{x_{\rm CH_4}}{x_{\rm H_2}^2} \cdot \left(\frac{P}{P_{\rm o}}\right)^{-1} \tag{7}$$

$$\begin{split} &\overline{h}_{2,C_xH_yO_z}^{\circ} + m_2 \cdot \overline{h}_{2,H_2O(l)}^{\circ} + (m_1 - m_2) \cdot \overline{h}_{2,H_2O(v)}^{\circ} + \lambda \cdot \overline{h}_{19,H_2O(v)}^{\circ} + q_{added} \\ &= \alpha_1 \overline{h}_{3,CH_4}^{\circ} + \alpha_2 \overline{h}_{3,H_2}^{\circ} + \alpha_3 \overline{h}_{3,CO}^{\circ} + \alpha_4 \overline{h}_{3,CO_2}^{\circ} + \alpha_5 \overline{h}_{3,H_2O}^{\circ} \end{split} \tag{8}$$

In a previous paper of the authors [11], a thermodynamic model of a direct internal reforming SOFC, which was based on 0-D modeling technique, was presented. In this paper, a better model for SOFC that includes the heat transfer mechanisms is used. Details on the model equations for the SOFC are available elsewhere [10]. The modeling technique and the main features of the heat transfer model of the SOFC used in this study are as follows:

- A control volume around the repeat element of a planar, coflow, and direct internal reforming SOFC is taken.
- Solid structure is modeled in 2-D, whereas gas channels are modeled in 1-D.
- Cell voltage, Reynolds number at the fuel channel inlet, and excess air coefficient are the main input parameters.
   Current density, temperature and molar gas composition distributions, fuel utilization, power output, and electrical efficiency of the cell are the main output parameters.
- Six gas species (CH<sub>4</sub>, H<sub>2</sub>, CO, CO<sub>2</sub>, H<sub>2</sub>O and N<sub>2</sub>) at the fuel channel inlet and two gas species (O<sub>2</sub> and N<sub>2</sub>) at the air channel inlet are considered.
- Fully developed laminar flow conditions are assumed in the air and fuel channels.
- Convection in the rectangular ducts, surface-to-surface radiation effects, conduction heat transfer at the section where the interconnects are in contact with Positive-Electrolyte-Negative (PEN) structure, and ohmic, activation and concentration polarizations are considered.
- The code is written in MatLAB.
- The model is validated with the results from IEA Benchmark Test [12].

Using the SOFC model discussed above, the code developed for the heat transfer model is run several times to obtain a desired fuel utilization for a given cell geometry, cell voltage, Reynolds number and excess air coefficient. Using this code, output for a single cell is obtained. For this output, number of stacks needed for the system can be calculated as follows:

$$n_{\text{stack}} = \frac{\dot{W}_{\text{req,SOFC}}}{w_{\text{SOFC}} \cdot n_{\text{cps}}} \tag{9}$$

We should take the closest integer higher than the value obtained by Eq. (9). Then, power output of SOFC and molar flow rate of gas species at the inlets and exits of fuel and air channels can be calculated for the total amount of stacks calculated.

At this point, we can calculate the molar flow rate of dry biomass entering the system using Eq. (10).

$$\dot{n}_{C_x H_y O_z} = \frac{\sum_{k=1}^{5} \dot{n}_{k, \text{fc.inlet}}}{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_4 + \alpha_5} \tag{10}$$

If we consider complete combustion in the afterburner, the chemical reaction occurring in the afterburner may be given as

$$\begin{split} \dot{n}_{6,\text{CH}_4}\text{CH}_4 + \dot{n}_{6,\text{H}_2}\text{H}_2 + \dot{n}_{6,\text{CO}}\text{CO} + \dot{n}_{6,\text{CO}_2}\text{CO}_2 + \dot{n}_{6,\text{H}_2\text{O}}\text{H}_2\text{O} \\ + \dot{n}_{6,\text{N}_2}\text{N}_2 + \dot{n}_{10,\text{O}_2}\text{O}_2 + \dot{n}_{10,\text{N}_2}\text{N}_2 \rightarrow \dot{n}_{11,\text{CO}_2}\text{CO}_2 + \dot{n}_{11,\text{H}_2\text{O}}\text{H}_2\text{O} \\ + \dot{n}_{11,\text{O}_2}\text{O}_2 + \dot{n}_{11,\text{N}_2}\text{N}_2 \end{split} \tag{11}$$

The molar flow rates of gas species at states 6 and 10 are known from the SOFC model. We can calculate the molar flow rates of gas species at state 11 using the atom balances, as given in Eqs. (12)–(15); and the enthalpy flow rate of this state can be found using an energy balance around the control volume enclosing the afterburner, as given in Eq. (16).

$$\dot{n}_{11,CO_2} = \dot{n}_{6,CH_4} + \dot{n}_{6,CO} + \dot{n}_{6,CO_2} \tag{12}$$

$$\dot{n}_{11,H_2O} = 2 \cdot \dot{n}_{6,CH_4} + \dot{n}_{6,H_2} + \dot{n}_{6,H_2O} \tag{13}$$

$$\dot{n}_{11,O_2} = \dot{n}_{6,CO}/2 + \dot{n}_{6,CO_2} + \dot{n}_{6,H_2O}/2 + \dot{n}_{10,O_2} - \dot{n}_{11,CO_2} - \dot{n}_{11,H_2O}/2 \quad (14)$$

$$\dot{n}_{11,N_2} = \dot{n}_{6,N_2} + \dot{n}_{10,N_2} \tag{15}$$

$$\dot{H}_{11} = \sum_{k=1}^{6} (\dot{n}_{6,k} \cdot \overline{h}_{6,k}) + \sum_{l=1}^{2} (\dot{n}_{10,l} \cdot \overline{h}_{10,l})$$
(16)

where k denotes  $CH_4$ ,  $H_2$ , CO,  $CO_2$ ,  $H_2O$  and  $N_2$ ; whereas l denotes  $O_2$  and  $N_2$ .

The specific enthalpy of state 8 may be written as:

$$\overline{h}_8 = \overline{h}_7 + \frac{(P_8 - P_7) \cdot M_{air}}{\rho_{air} \cdot \eta_{blower}} \tag{17}$$

Specific work input to blower may be given as

$$\dot{W}_{blower} = (\dot{n}_{9,O_2} + \dot{n}_{9,N_2}) \cdot (\overline{h}_8 - \overline{h}_7) \tag{18}$$

From an energy balance around the control volume enclosing the heat exchanger, enthalpy flow rate of state 12 may be found as:

$$\dot{H}_{12} = \dot{H}_{11} + \sum_{l=1}^{2} (\dot{n}_{8,l} \cdot \overline{h}_{8,l}) - \sum_{l=1}^{2} (\dot{n}_{9,l} \cdot \overline{h}_{9,l})$$
(19)

From an energy balance around the control volume enclosing the dryer, enthalpy flow rate of state 13b may be found as

$$\begin{split} \dot{H}_{13b} &= \sum_{m=1}^{4} \left( \dot{n}_{11,m} \cdot \overline{h}_{14,m} \right) + \dot{n}_{C_x H_y O_z} \cdot \left( \overline{h}_{2,C_x H_y O_z} + m_2 \cdot \overline{h}_{2,H_2 O(l)} \right. \\ &+ \left. \left( m_1 - m_2 \right) \cdot \overline{h}_{2,H_2 O(v)} - \overline{h}_{1,C_x H_y O_z} - m_1 \cdot \overline{h}_{1,H_2 O(l)} \right) \end{split} \tag{20}$$

where m denotes  $CO_2$ ,  $H_2O$ ,  $O_2$  and  $N_2$ .

The specific enthalpy for state 16 may be written as

$$\overline{h}_{16} = \overline{h}_{15} + \frac{\nu_{15} \cdot (P_{16} - P_{15}) \cdot M_{H_2O}}{\eta_{\text{pump}}}$$
 (21)

At this point, we can calculate the total heat added to the gasifier as:

$$\dot{Q}_{added} = q_{added} \cdot \dot{n}_{C_x H_y O_z} \tag{22}$$

Enthalpy flow rate of state 13a can be calculated as

$$\dot{H}_{13a} = \dot{H}_{13b} + \dot{Q}_{added} \tag{23}$$

From an energy balance around the control volume enclosing the steam generator, the molar flow rate of steam generated may be found as

$$\dot{n}_{17} = \frac{\dot{H}_{12} - \dot{H}_{13a}}{\overline{h}_{17} - \overline{h}_{16}} \tag{24}$$

Work input to pump may be given as

$$\dot{W}_{\text{pump}} = \dot{\eta}_{17} \cdot (\overline{h}_{16} - \overline{h}_{15}) \tag{25}$$

Change of enthalpy flow rate of the process may be shown as

$$\Delta \dot{H}_{\text{process}} = (\dot{n}_{17} - \dot{n}_{C_v H_v O_z} \cdot \lambda) \cdot (\overline{h}_{18} - \overline{h}_{15}) \tag{26}$$

Net electrical power output of the system may be given as

$$\dot{W}_{\text{net}} = n_{\text{stack}} \cdot n_{\text{cps}} \cdot w_{\text{SOFC}} \cdot \eta_{\text{inv}} - \dot{W}_{\text{blower}} - \dot{W}_{\text{pump}}$$
(27)

Electrical efficiency, fuel utilization efficiency, and power-to-heat ratio may be calculated using Eqs. (28)–(30), respectively.

$$\eta_{\rm el} = \frac{\dot{W}_{\rm net}}{\dot{n}_{\rm C_xH_VO_Z} \cdot (\rm LHV + m_1 \cdot \overline{h}_{fg})} \tag{28}$$

$$FUE = \frac{\dot{W}_{net} + \Delta \dot{H}_{process}}{\dot{n}_{C_x H_y O_z} \cdot \left(LHV + m_1 \cdot \overline{h}_{fg}\right)} \tag{29}$$

$$PHR = \frac{\dot{W}_{\text{net}}}{\Delta \dot{H}_{\text{process}}}$$
 (30)

After energy analysis is completed, exergy analysis is conducted. In this analysis, exergy balance which is derived by combining first and second laws of thermodynamics [13] is applied to the control volumes enclosing the components. The steady state form of control volume exergy balance may be given as

$$0 = \sum_{i} \left( 1 - \frac{T_o}{T_i} \right) \cdot \dot{Q}_j - \dot{W}_{cv} + \sum_{i} \dot{n}_i \cdot ex_i - \sum_{e} \dot{n}_e \cdot ex_e - \dot{E}x_D$$
 (31)

In Eq. (31), ex represents the specific molar exergy. The components of specific exergy are discussed below.  $\dot{E}x_D$  represents the exergy destruction in the control volume. Exergy losses are included in the fourth term of Eq. (31).

If we neglect the magnetic, electrical, nuclear, kinetic and potential effects, there are mainly two types of exergy: pyhsical and chemical. The first one measures the amount of work when the system comes into thermal ( $T=T_o$ ) and mechanical ( $P=P_o$ ) equilibrium. This condition is called as restricted dead state. Chemical exergy gives the amount of work when the system is brought from restricted dead state to dead state. At dead state, in addition to the thermal and mechanical equilibrium, the system is also at chemical equilibrium ( $\mu=\mu_o$ ).

The physical flow exergy for simple, compressible pure substances is given as:

$$ex^{PH} = (h - h_o) - T_o(s - s_o)$$
 (32)

Chemical exergy may be found using the tables available in the literature [14]. For an ideal gas mixture, Eq. (33) can be used to calculate the specific molar chemical exergy of the mixture.

$$ex^{CH} = \sum x_k \cdot e\overline{x}_k^{CH} + \overline{R} \cdot T_o \cdot \sum x_k \cdot lnx_k \tag{33}$$

The exergy destruction rate in a component may be compared to the exergy rate of the fuel provided to the overall system using the exergy destruction ratio, as follows:

$$y_{\rm D} = \frac{\dot{E}x_{\rm D}}{\dot{E}x_{\rm F}} \tag{34}$$

The exergy destruction rate of a component may be compared to the total exergy destruction rate within the system using the following equation:

$$y_{\mathrm{D}}^{*} = \frac{\dot{\mathrm{E}}x_{\mathrm{D}}}{\dot{\mathrm{E}}x_{\mathrm{D,tot}}} \tag{35}$$

The exergy loss ratio is used to compare the exergy loss rate to the exergy rate of the fuel provided to the overall system.

$$y_{L} = \frac{\dot{E}x_{L}}{\dot{E}x_{F}} \tag{36}$$

In defining the exergetic efficiency, it is necessary to identify both a product and a fuel for the thermodynamic system being analyzed. The product represents the desired output produced by the system. The fuel represents the resources expended to generate the product. Exergetic efficiency of a component or system may be given as

$$\varepsilon = \frac{\dot{E}_{P}}{\dot{E}_{P}} = 1 - \frac{\dot{E}_{D} + \dot{E}_{L}}{\dot{E}_{P}} \tag{37}$$

Exergetic efficiency of the system can also be defined in terms of exergy destruction ratio and exergy loss ratio.

$$\varepsilon = 1 - \sum y_D - \sum y_L \tag{38}$$

For the integrated system studied in this paper, exergetic efficiency of the system may be defined as:

$$\varepsilon = \frac{\dot{W}_{net} + \Delta \dot{E} x_{process}}{\dot{E} x_{ch,C_xH_yO_z} + \dot{n}_{15} \cdot \overline{e}_{ch,H_2O(l)}} \tag{39}$$

 $\dot{E}x_{ch,C_xH_yO_z}$  can be found using the correlation given by Szargut [14]. The correlation is modified for this study as follows:

$$\dot{E}x_{ch,C_xH_yO_z} = \beta \cdot \left[ \dot{n}_{C_xH_yO_z} \cdot \left( LHV + m_1 \cdot \overline{h}_{fg} \right) \right] \tag{40}$$

where  $\beta$  is defined for solid C,H,O,N compounds (for O/C < 2) as [14]

$$\beta \hspace{-0.05cm} = \hspace{-0.05cm} \frac{1.044 + 0.016 \cdot H/C - 0.3493 \cdot O/C \cdot (1 + 0.0531 \cdot H/C) + 0.0493 \cdot N/C}{1 - 0.4124 \cdot O/C}$$

(41)

Change of exergetic rate of process may be given as

$$\Delta \dot{E} x_{\text{process}} = (\dot{n}_{17} - \dot{n}_{C_x H_y O_z} \cdot \lambda) \cdot (e x_{18} - e x_{15}) \tag{42}$$

More information on exergy and its applications can be found in [15].

# 4. Results and discussion

The input data used in this study are shown in Table 1. Using this data, syngas composition is first calculated and shown in Table 2. As it can be seen from this table, when enriched

Table 1 – Input data.	
Environmental temperature	25 °C
	25 G
Fuel	TTT 1
Type of biomass	Wood
Ultimate analysis of biomass	50% C, 6% H, 44% O
[%wt dry basis]	40%
Moisture content in biomass [%wt]	40 /0
Gasifier	
Moisture content in biomass entering	20%
gasifier [%wt]	
Temperature of syngas exiting gasifier	900 °C
Molar ratio of steam entering to gasifier to	0.1
dry biomass	050/ 0 650/ 34
Molar composition of enriched oxygen	35% O <sub>2</sub> , 65% N <sub>2</sub>
SOFC	
Power requirement of SOFC	10 kW
Number of cells per stack	50
Temperature of syngas entering SOFC	850 °C
Temperature of air entering SOFC	850 °C
Pressure of the cell	1 atm
Cell voltage	0.65
Excess air coefficient	7
Active cell area	$10 \times 10 \text{ cm}^2$
Number of repeat elements per	18
single cell Flow configuration	Co-flow
Manufacturing type	Electrolyte-supported
Thickness of air channel	0.1 cm
Thickness of fuel channel	0.1 cm
Thickness of interconnect	0.3 cm
Thickness of anode	0.005 cm
Thickness of electrolyte	0.015 cm
Thickness of cathode	0.005 cm
Emissivity of PEN	0.8
Emissivity of interconnect	0.1
Diffusivity of anode	0.91 cm <sup>2</sup> /s
Diffusivity of cathode	$0.22 \text{ cm}^2/\text{s}$
Porosity of anode	0.5
Porosity of cathode	0.5
Turtuosity of anode	4
Turtuosity of cathode	4
Balance of plant	
Temperature of exhaust gas leaving the system	127 °C
Pressure ratio of blowers	1.18
Isentropic efficiency of blowers	0.53
Pressure ratio of pump	1.2
Isentropic efficiency of pump	0.8
Inverter efficiency	0.95

oxygen is used instead of air, molar ratio of all species except nitrogen increases due to sending less amount of nitrogen to the gasifier. In the case of using steam as gasification agent, the molar ratios of gases that are used as fuel in SOFC, i.e. CH<sub>4</sub>,

Table 2 – Syngas	comp	osition	(mola	basis)		
	$x_{\text{CH}_4}$	$x_{H_2}$	$x_{CO}$	$x_{CO_2}$	$x_{H_2O}$	$x_{N_2}$
Case1: Air	0.14%	11.22%	8.16%	12.95%	22.68%	44.84%
Case2: Enriched O <sub>2</sub>	0.28%	15.74%	11.40%	16.37%	28.80%	27.41%
Case3: Steam	2.15%	43.37%	27.38%	8.98%	18.12%	0.00%

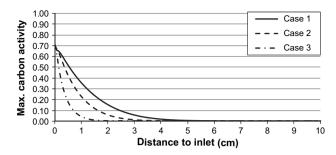


Fig. 2 - Change of maximum carbon activity with distance.

 $\rm H_2$  and CO, are higher than the cases when we use air or enriched oxygen; however the molar ratio of  $\rm H_2O$  is lower than the other cases according to chemical equilibrium calculations.

After finding the syngas composition, heat transfer model of the SOFC is used to find the fuel cell related output parameters. First, recirculation ratio is taken as zero and the code is run until a fuel utilization of 0.85 is obtained. At this point, the maximum carbon activity through the channel length is checked. If this value is less than 1 for all the nodes, then there is no carbon deposition problem. If this value is higher than 1 for any nodes, then the calculations should be repeated with higher recirculation ratios until the carbon deposition is prevented. Fig. 2 shows that maximum carbon activity is less than 1 for all the nodes for all cases even if we do not recirculate the depleted fuel.

Fig. 3 shows the current density distribution for each case. Since the molar ratio of gas species used as fuel in SOFCs, e.g. CH<sub>4</sub>, H<sub>2</sub> and CO, is higher for case-3, higher current densities for each node are obtained for this case compared to other cases. From Table 3, it can be seen that average current densities for cases 1, 2, and 3 are 0.240, 0.246, and 0.343 A/cm<sup>2</sup>, respectively. It can also be followed from this table that power density for case-3 is higher than the other cases because we consider the cell voltage as constant in the modeling and average current density is higher for case-3 than other cases. It is also found that 13 stacks are needed for cases 1 and 2, whereas only 9 stacks are needed for case-3. This result shows that the purchase equipment cost for case-3 is lower than the other cases.

2-D temperature distributions of SOFCs are given in Figs. 4–6. From these figures, it is seen that temperature gradient in the flow direction is the highest in case-3. Case-2 and case-1 follow it, respectively. It should be noted that the temperature

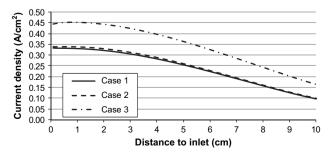


Fig. 3 - Change of current density with distance.

Table 3 – Recirculation ratio, Reynolds Number, average current density, fuel utilization ratio, number of stacks.

	r	Re	i <sub>c,ave</sub> [A/cm <sup>2</sup> ]	$U_{\mathrm{F}}$	W <sub>sofc</sub> [W/cm <sup>2</sup> ]	n <sub>stack</sub>
Case1: Air	0	10.0	0.240	0.85	0.156	13
Case2: Enriched O <sub>2</sub>	0	6.5	0.246	0.85	0.160	13
Case3: Steam	0	1.5	0.343	0.85	0.223	9

gradients are still less than the maximum allowable value that could cause thermomechanical instability.

Mass flow rates of substances entering the system are given in Table 4. It can be seen in this table that, for case-1, we need to feed more biomass to the system, which increases the cost of fuel. In addition, wood needs to be cut into small pieces before feeding to the system, hence equipment and operation cost for pretreatment of wood increases for this case. The energy input for the pretreatment operation of wood also increases. However, it should be noted that pretreatment of wood except drying is not taken into account in the analyses. From Table 4, the mass flow rate of air and water fed to the system, and steam produced and sent to the users can be seen. For case-3, fewer amounts of air and water are fed to the system, which in turn decreases the costs associated with the operation of blowers and pump. However, less amount of steam is produced for this case due to sending high amount of steam to the gasifier for initiating the gasification reactions.

Power input to the auxiliary components and power output from the system are shown in Table 5. It can be followed from this table that net power output for case-2 is the highest, which is mainly due to higher amount of power obtained for the given number of stacks. Change of enthalpy rate of the process is found to be the highest for case-1 and lowest for case-3. This is because allothermal gasification is used in case-3 and considerable amount of energy is spent in the gasification process, hence less energy remains for producing steam.

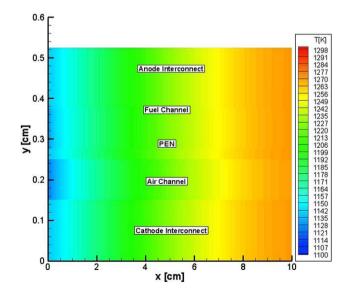


Fig. 4 – 2-D temperature distribution of SOFC for case-1 (Air gasification).

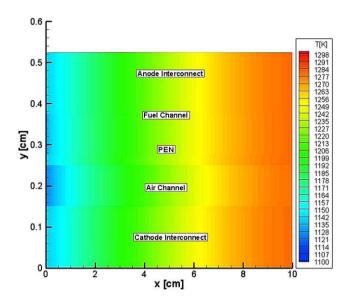


Fig. 5 – 2-D temperature distribution of SOFC for case-2 (Enriched oxygen gasification).

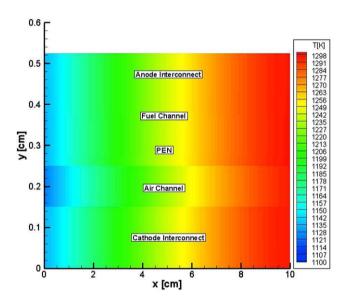


Fig. 6 – 2-D temperature distribution of SOFC for case-3 (Steam gasification).

Electrical efficiency, fuel utilization efficiency, power-to-heat ratio, and exergetic efficiency are chosen as performance assessment parameters in this study. The values of these parameters are shown in Table 6. It can be seen from this table that case-3 has the highest electrical efficiency. However, it

Table 4 – Mass flow rate of substances entering the system.						
	ṁ <sub>biomass</sub> [g/s]	ṁ <sub>air</sub> (В1) [g/s]	ṁ <sub>air</sub> (В2) [g/s]	m <sub>water</sub> [g/s]	ḿ <sub>steam</sub> [g/s]	
Case1: Air	4.048	7.796	45.648	7.654	7.654	
Case2: Enriched O <sub>2</sub>	3.867	6.989	46.841	6.604	6.604	
Case3: Steam	1.826	-	45.219	0.767	0.685	

has also the lowest fuel utilization efficiency since considerable amount of steam is sent to the gasifier and less steam is sent for process heating purposes. In general, producing electricity is more expensive than producing heat. If we compare the power-to-heat ratios, we can see that case-3 is the highest. It may be interpreted from this result that the primary purpose of using the system in case-3 should be producing electricity rather than producing heat. Exergetic efficiency is another way of comparing the overall system performance. In this comparison, the quality of the energy forms together with the quantity of the energy forms is considered. It is seen from Table 6 that exergetic efficiency for case-3 is the highest. When we combine all the results for performance assessment parameters, we can conclude that steam should be selected as the gasification agent to have a better performance of the system.

We can also use air and steam or enriched oxygen and steam gasification agents in the integrated SOFC and biomass gasification systems. In these systems, molar ratio of oxidant to dry biomass and molar ratio of steam to dry biomass may be altered to get different results. However, we expect that such output parameters will be between those obtained from only when one of the gasification agents is used. For example, if we choose enriched oxygen and steam gasification case, it is expected that the electrical efficiency will be between 19.9% and 41.8% and fuel utilization efficiency will be between 50.8% and 60.9%, based on the efficiencies shown in Table 6.

Exergy destructions in the components and exergy destruction ratios are calculated and the results are shown in Tables 7 and 8. The results show that, for cases 1 and 2, the largest portion of exergy is destructed in the gasifier. This destruction accounts for 31.02% for case-1 and 30.89% for case-2 of the exergy of the fuel, and 48.60% for case-1 and 48.15% for case-2 of the total exergy destructions. For case-3, the magnitude of exergy destruction for gasifier is much lower than that for cases 1 and 2 because of using allothermal gasification for this case. In this case, the highest exergy is destructed in the heat exchanger, which is 25.65% of the exergy of the fuel and 46.44% of the total exergy destructions. Exergy losses to the environment are also calculated. The exergy losses are found as 2676 W, 2489 W, and 1281 W for cases 1, 2, and 3, respectively. When we compare the exergy loss ratios, it is seen that case-3 has

Table 5 – Power demand for auxiliary components, net power and heat output.							
	$\dot{W}_{SOFC}$ [W]	$\dot{W}_{blower-1}$ [W]	$\dot{W}_{blower-2}$ [W]	$\dot{W}_{pump}$ [W]	$\dot{W}_{net}$ [W]	$\Delta \dot{H}_{process}$ [W]	
Case1: Air Case2: Enriched O <sub>2</sub>	10140 10384	227.5 204.0	1332.1 1366.9	0.2 0.2	8073.2 8293.7	19741.3 17032.9	
Case3: Steam	10031	-	1319.6	0.02	8233.7	1765.9	

Table 6 – Performance assessment parameters.					
	$\eta_{ m el}$	FUE	PHR	ε	
Case1: Air	18.5%	63.9%	0.409	30.9%	
Case2: Enriched O <sub>2</sub>	19.9%	60.9%	0.487	30.7%	
Case3: Steam	41.8%	50.8%	4.649	39.1%	

Table 7 – Exergy destructions in the components.							
Component	Exe	Exergy destruction [W]					
	Case 1	Case 2	Case 3				
SOFC	664	692	845				
Gasifier	15727	14952	837				
Afterburner	1622	1800	1490				
Dryer	3018	2884	1336				
Gas cleanup	678	507	164				
Heat exchanger	6421	6453	5834				
Blower-1	217	195	-				
Blower-2	1272	1305	1260				
ASU	-	4	-				
Steam generator	2235	1740	295				
Water pump	0	0	0				
Inverter	507	519	502				

Table 8 – Exergy destruction ratios.						
	Cas	e 1	Case 2		Case 3	
	y <sub>D</sub> [%]	y <sub>D</sub> *[%]	y <sub>D</sub> [%]	y <sub>D</sub> * [%]	y <sub>D</sub> [%]	y <sub>D</sub> * [%]
SOFC	1.31	2.05	1.43	2.23	3.71	6.72
Gasifier	31.02	48.60	30.89	48.15	3.67	6.67
Afterburner	3.20	5.01	3.72	5.80	6.55	11.86
Dryer	5.95	9.33	5.96	9.29	5.88	10.64
Gas cleanup	1.34	2.09	1.05	1.63	0.72	1.30
Heat exchanger	12.66	19.84	13.33	20.78	25.65	46.44
Blower-1	0.43	0.67	0.40	0.63	0.00	0.00
Blower-2	2.51	3.93	2.70	4.20	5.54	10.03
ASU	-	-	0.00	0.01	0.00	0.00
Steam generator	4.41	6.91	3.59	5.61	1.30	2.35
Water pump	0.00	0.00	0.00	0.00	0.00	0.00
Inverter	1.00	1.57	1.07	1.67	2.21	3.99

the highest exergy loss ratio, which is equal to the 5.63% of the exergy of the fuel. Case-1 (5.28%) and case-2 (5.14%) follow it, respectively.

#### 5. Conclusions

An analysis for integrated SOFC and biomass gasification systems is developed. For this purpose, a heat transfer model for the SOFC part and thermodynamic models for the rest of the components are used. The effect of gasification agent on the performance of the system is discussed. This study shows that using steam as the gasification agent yields the highest electrical efficiency, power-to-heat ratio and exergetic efficiency, but the lowest fuel utilization efficiency. It is also found that the largest portion of exergy is destructed at the gasifier for air and enriched oxygen gasification cases and the heat exchanger used for heating the air entering the SOFC for steam gasification case.

# Acknowledgment

The financial and technical support of an Ontario Premier's Research Excellence Award, the Natural Sciences and Engineering Research Council of Canada, EcoEnergy Technology Initiative Program, AAFC-NRC Bioproducts Program, Carleton University and University of Ontario and Institute of Technology is gratefully acknowledged.

#### Nomenclature

С	weight percentage of carbon in biomass
ex	specific molar exergy, J/mole
Ėx	exergy flow rate, W
FUE	fuel utilization ratio
h	specific molar enthalpy, J/mole
Н	weight percentage of hydrogen in biomass
Ĥ	enthalpy flow rate, W
K	chemical equilibrium constant
LHV	lower heating value, J/mole
m	molar ratio of water to dry biomass
M	molecular weight, g/mole
n	number
'n	molar flow rate, mole/s
N	weight percentage of nitrogen in biomass
0	weight percentage of oxygen in biomass
P	pressure, bar
PHR	power-to-heat ratio
q	specific molar heat, J/mole
q Ċ	heat rate, W
R	universal gas constant, J/mole-K
T	temperature, K
у	exergetic ratio
w	power output of a single cell, W
Ŵ	power output, W
х	molar concentration

#### G

Greek lett	ers
ρ	density, g/cm <sup>3</sup>
$\eta$	efficiency
$\Delta \overline{g}$	change in specific molar gibbs free energy, J/mole
υ	specific volume, cm³/g
3	exergetic efficiency
β	exergetic correlation constant
λ	molar ratio of steam entering the gasifier to the dry
	biomass
μ	chemical potential, J/mole

### Subscripts

cps	cell per stack
CV	control volume
D	destruction

el electrical inv inverter F fuel fc fuel cell

fg difference in property for saturated vapor and

saturated liquid

L loss m methar

m methanation
o standard
P product
req required
tot total

wgs water gas shift reaction

#### Superscripts

CH chemical PH physical

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